

# N-body simulations and Galactic Structure

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## Cosmological framework

The Standard Model of the Universe, as derived from data on large scale structures, distant supernovae, CMB, etc. predicts a flat, accelerating Universe

**predicts the existence of**

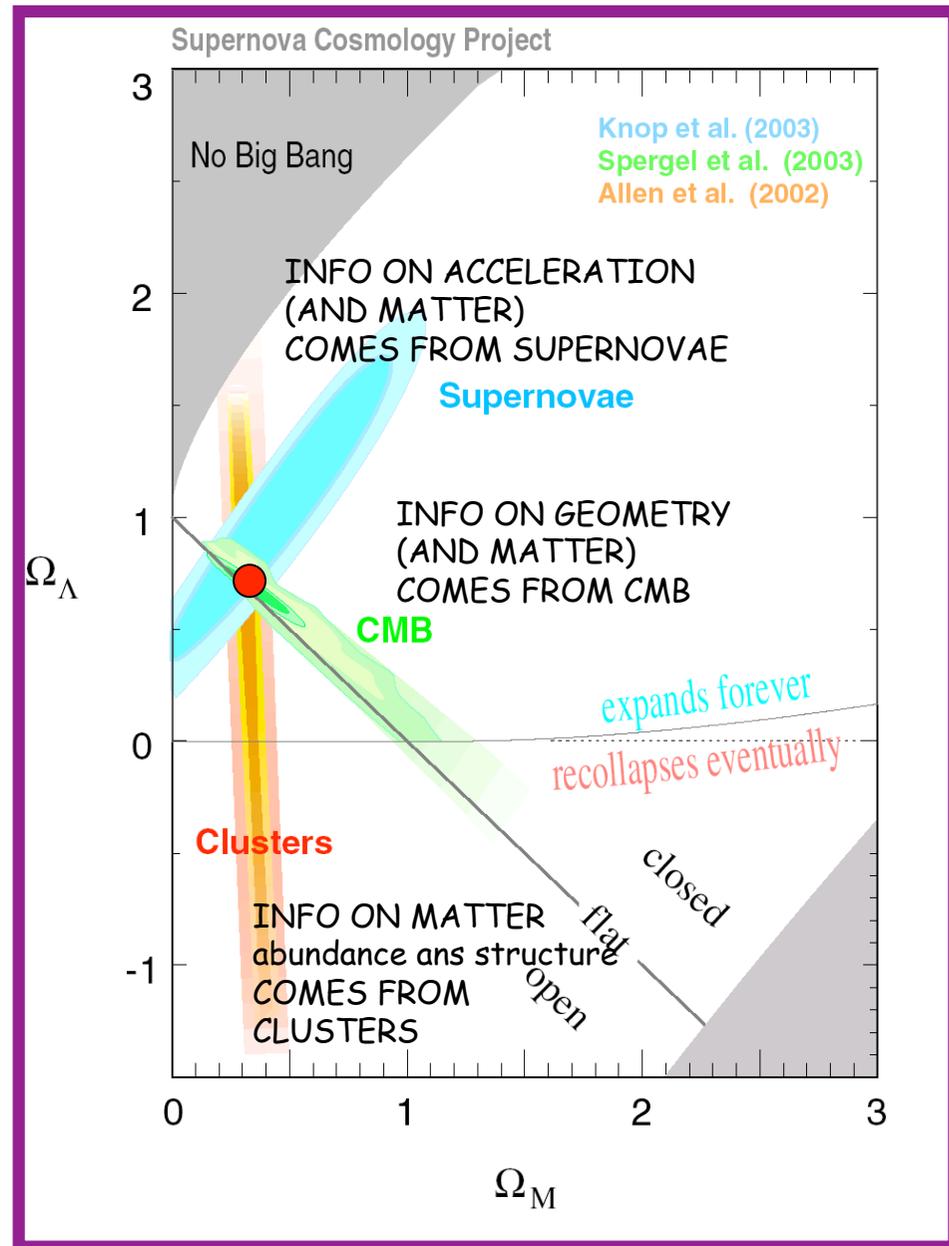
- an unknown form of repulsive energy, or dark energy

$$\Omega_{\Lambda} \sim 0.73$$

- an unknown type of non baryonic matter, or

**DARK MATTER**

$$\Omega_{DM} \sim 0.23$$



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$$\Omega_{DM} \sim 0.23$$

$$\Omega_{\text{tot}} \equiv \frac{\overset{\text{known particles}}{\rho_{\gamma}} + \overset{\text{unknown}}{\rho_{\nu}} + \rho_b + \rho_{DM} + \rho_{\Lambda}}{\rho_c} \sim 1$$

value for a flat universe

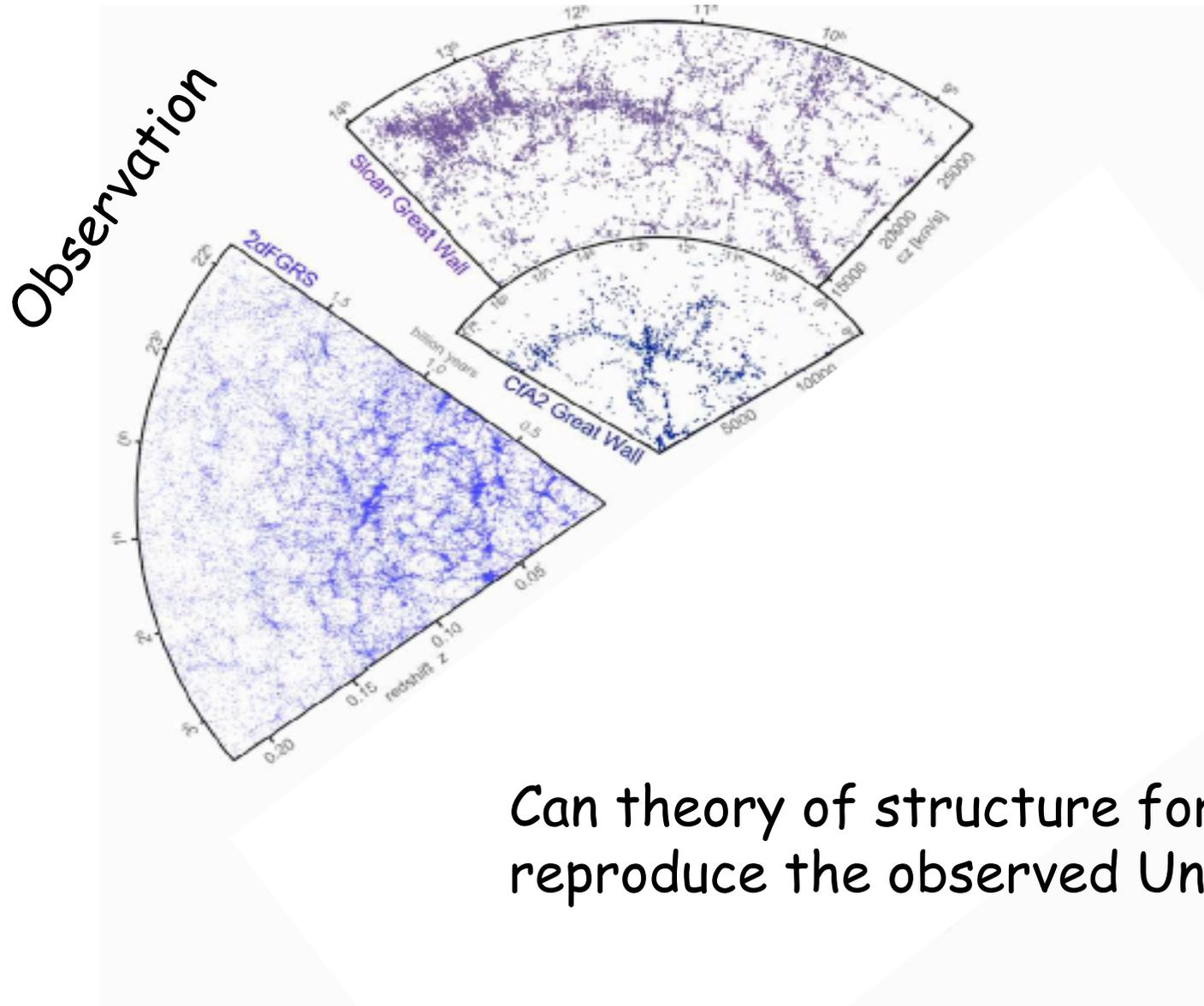
**VS the observed minor components**

$$\Omega_b \sim 0.005 \text{ (galaxies)}$$
$$\sim 0.04 \text{ (BBN)}$$

$$\Omega_{\gamma} \sim 10^{-5}$$

$$1.2 \cdot 10^{-3} < \Omega_{\nu} < 1.5 \cdot 10^{-2}$$

Infos on matter abundance and structure come from large scale structure observation



# Theory of structure formation and N-body simulations

## DM halos

Primordial density fluctuations grow and collapse in gravitationally bound structures which eventually virialize and form halos.

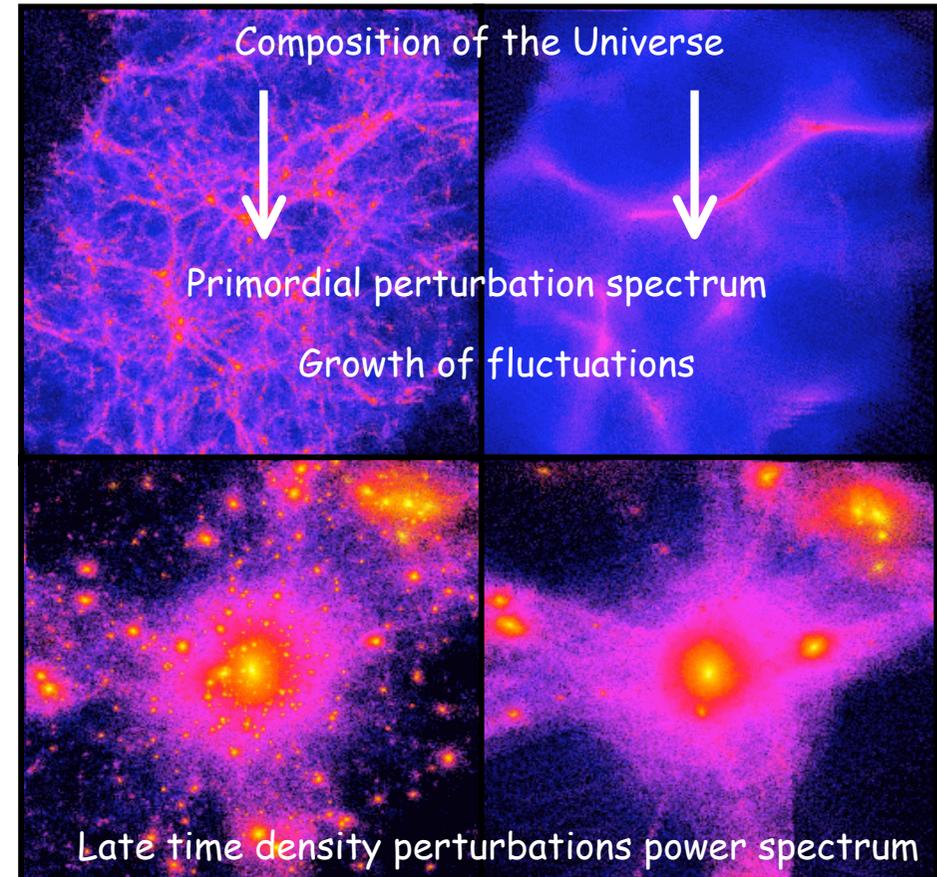
Particle nature of DM determines primordial power spectrum and assembly history.

Baryons are captured in the dark matter potential well and form galaxies, clusters, etc.

Once the power spectrum is fixed, the evolution is driven by gravitational force, and can be followed via numerical N-body simulations.

non-relativistic particles  
form smaller halos

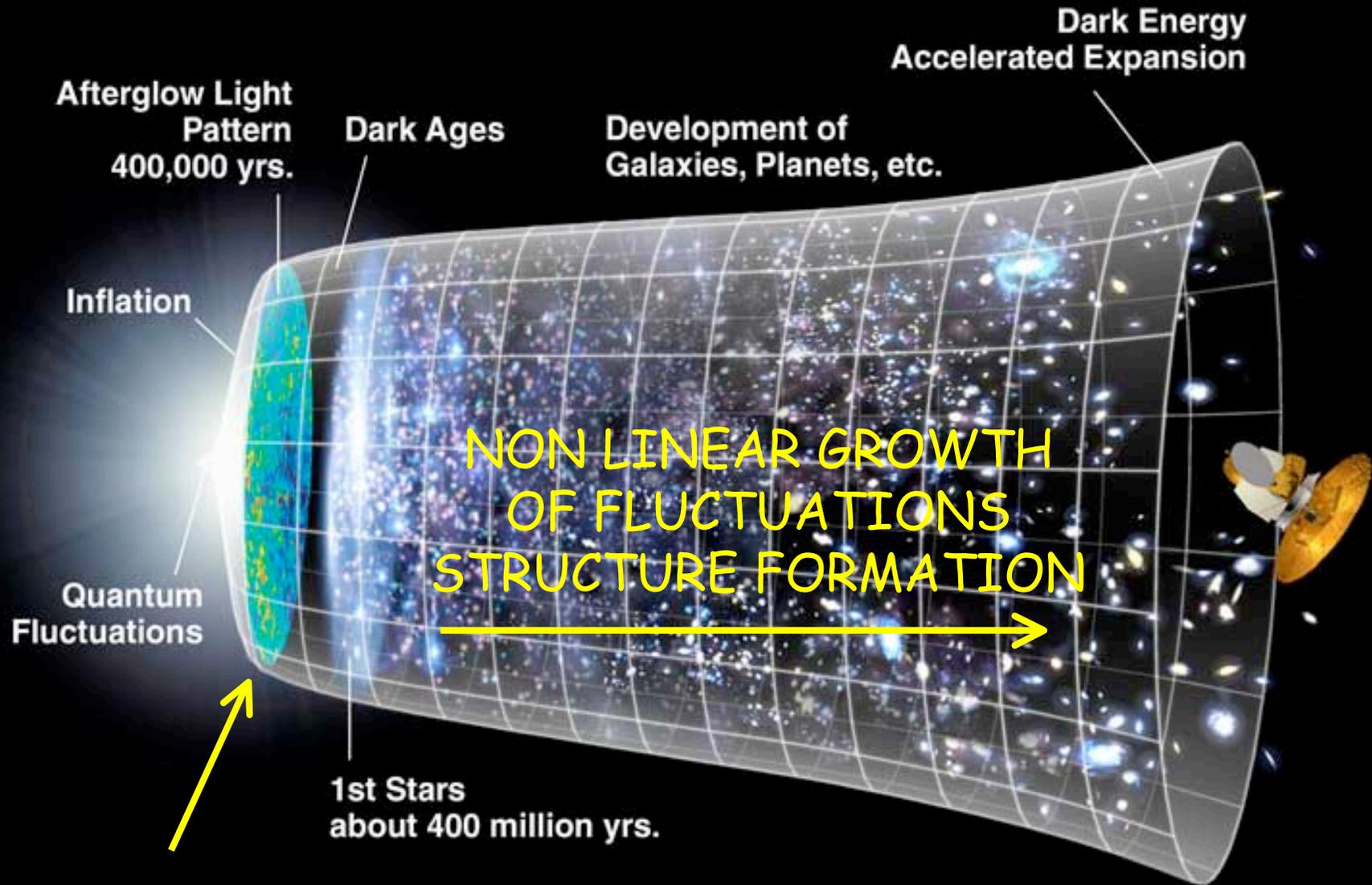
relativistic particles  
have larger kinetic energy  
and need larger mass  
to be gravitationally bound



Cold dark matter

Hot dark matter

# The thermal history of the universe



**NON LINEAR GROWTH  
OF FLUCTUATIONS  
STRUCTURE FORMATION**



**CMB physics**  
Universe is "mostly"  
homogeneous and isotropic, but seeds of structures are already there

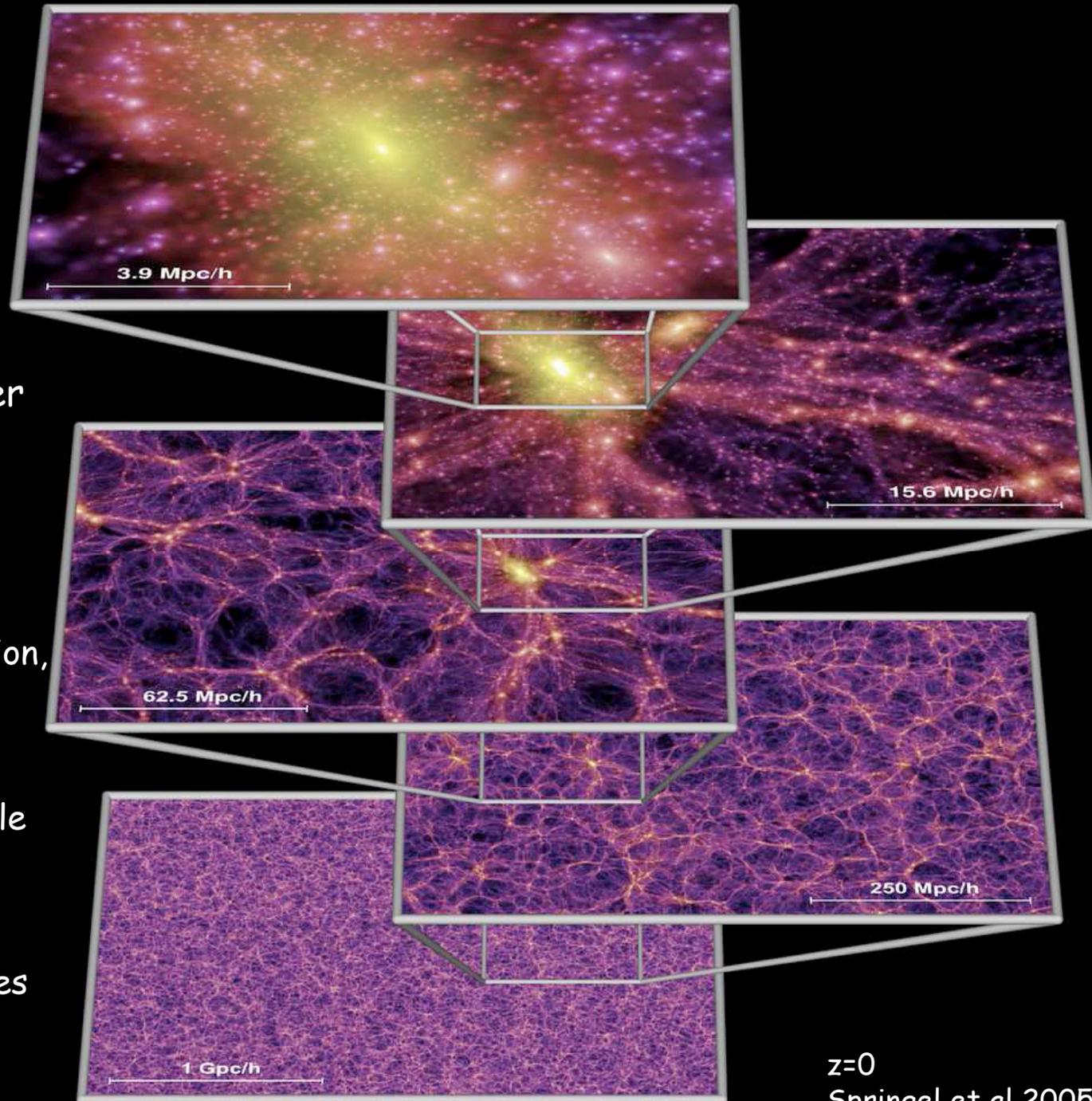
**Big Bang Expansion**

**13.7 billion years**

# MILLENNIUM Simulation CDM universe

Simulates halos  
on cosmological  
scales, then  
resimulates a smaller  
patch with higher  
mass resolution.

Tracks the formation  
of galaxies and  
quasars in the simulation,  
by implementing a  
semianalytic model  
to follow gas, star and  
supermassive black hole  
processes within the  
merger history trees  
of dark matter halos  
and their substructures

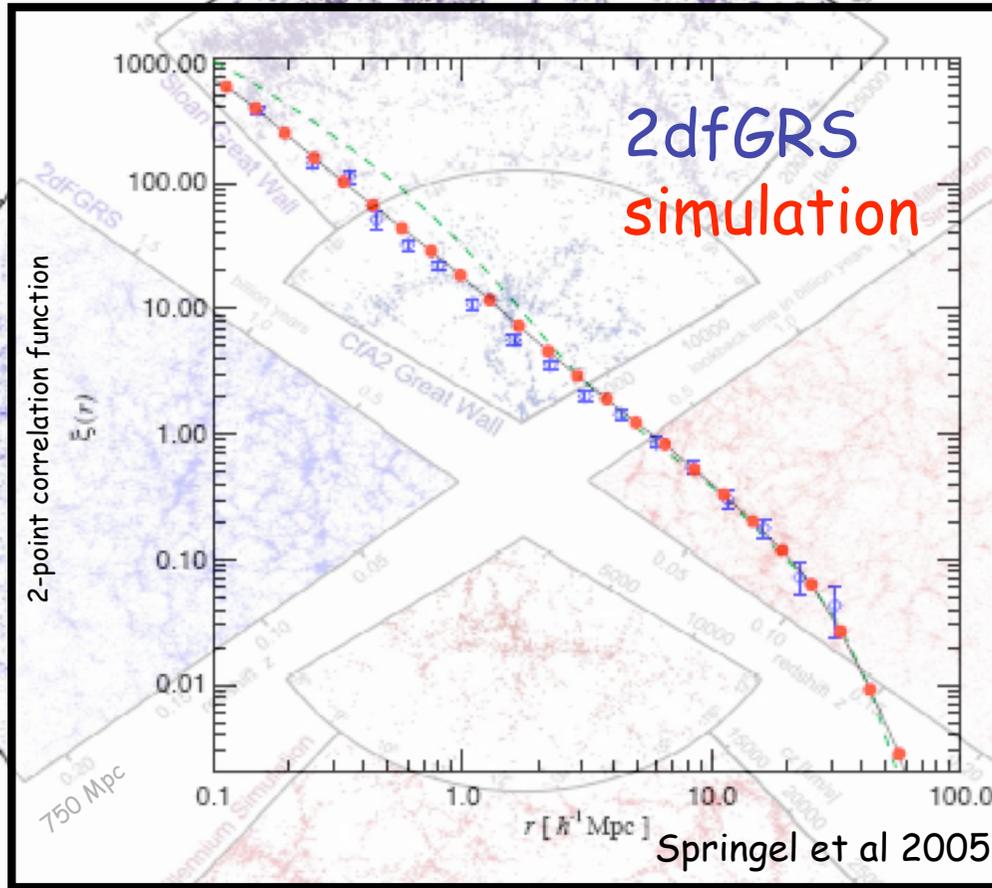


$z=0$   
Springel et al 2005



CDM N-body simulations better reproduce the data

Observation



CDM simulation  
(Millennium)

CDM  
> a few GeV

375 eV WDM

175 eV WDM

z=3

...YET

the warm dark matter  
scenario is not excluded  
since observations  
(clusters + Lyman  $\alpha$ )  
can probe

z=2

the universe only down  
to the dwarf scale

(which is the same scale as the CDM N-body sims)

z=1

Bode et al, 2001

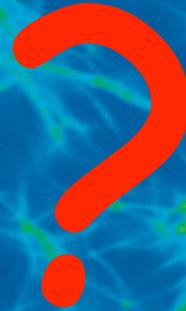
CDM  
> a few GeV

375 eV WDM

175 eV WDM

z=3

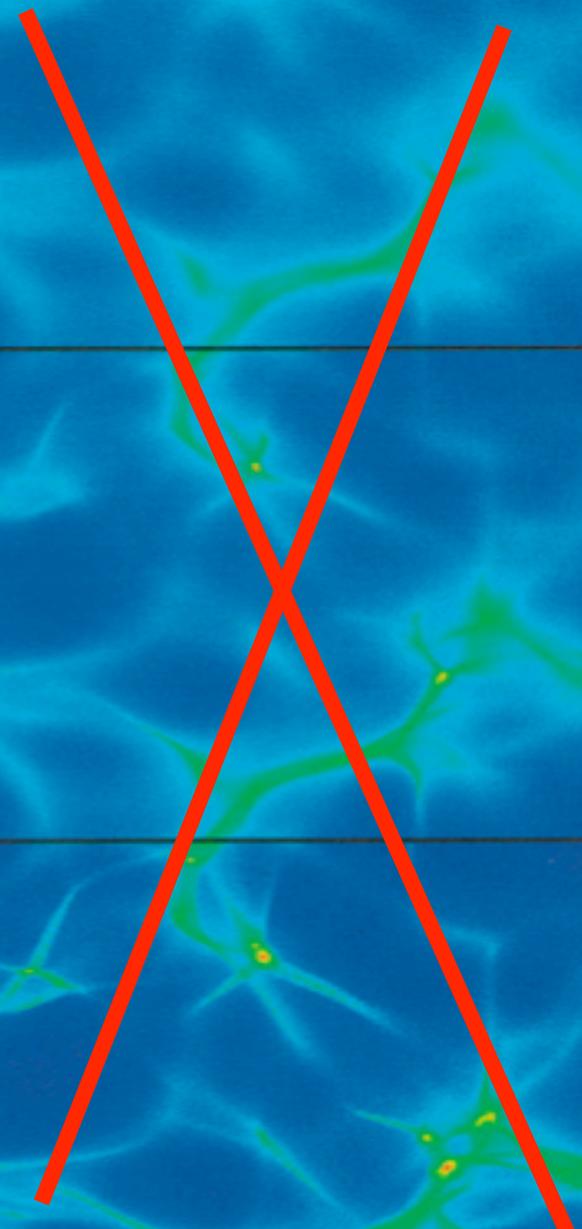
z=2



A 6 keV WDM  
would give a damping scale  
of  $10^7 M_{\text{sun}}$ , e.g. the  
dwarf scale

current limits depend on the particle  
z=1 and are around a few keV (Viel et al 2008)

Bode et al, 2001



CDM

375 eV WDM

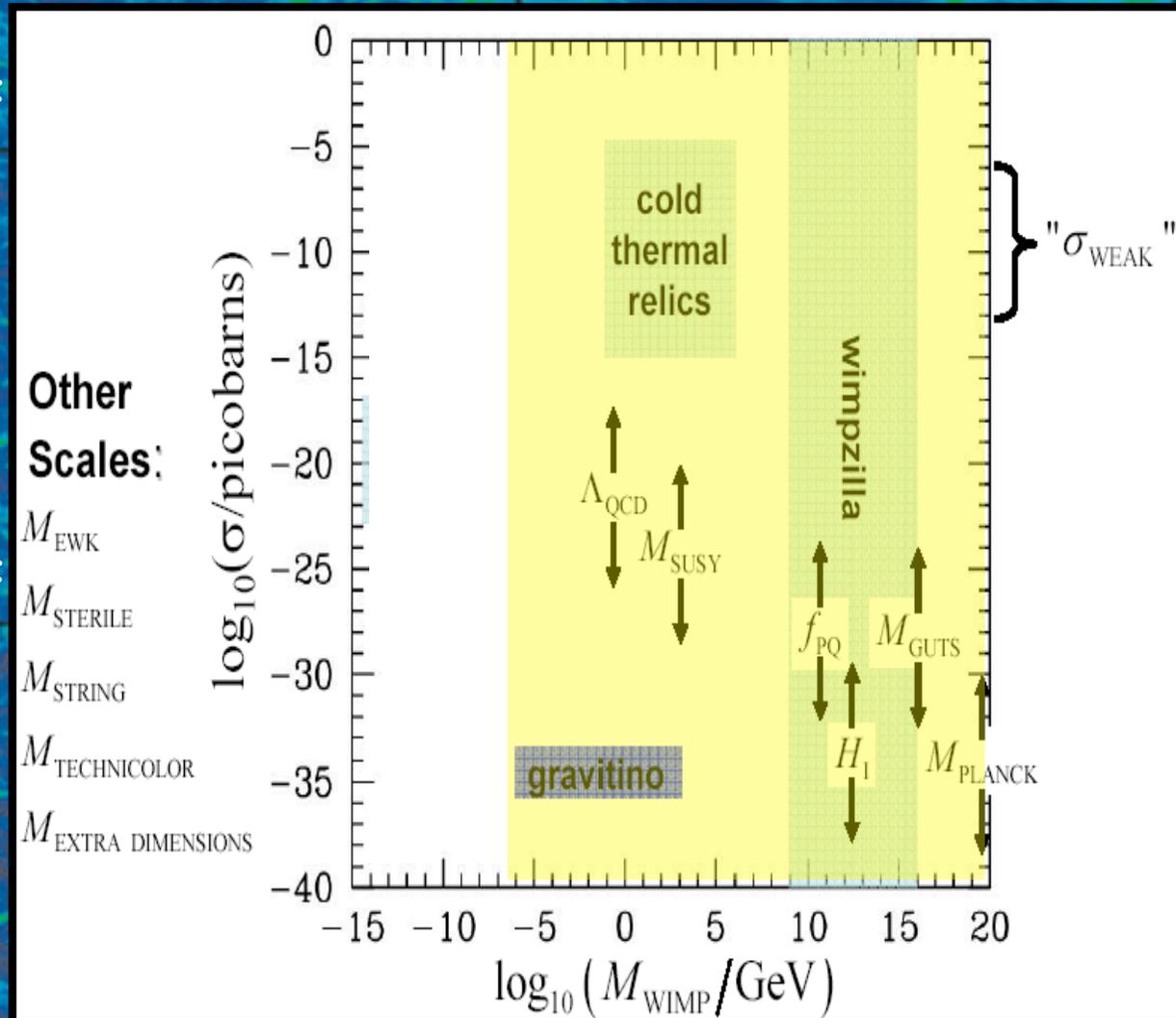
175 eV WDM

Plus, this is plausible for Particle Physics

$z=$

$z=$

$z=1$

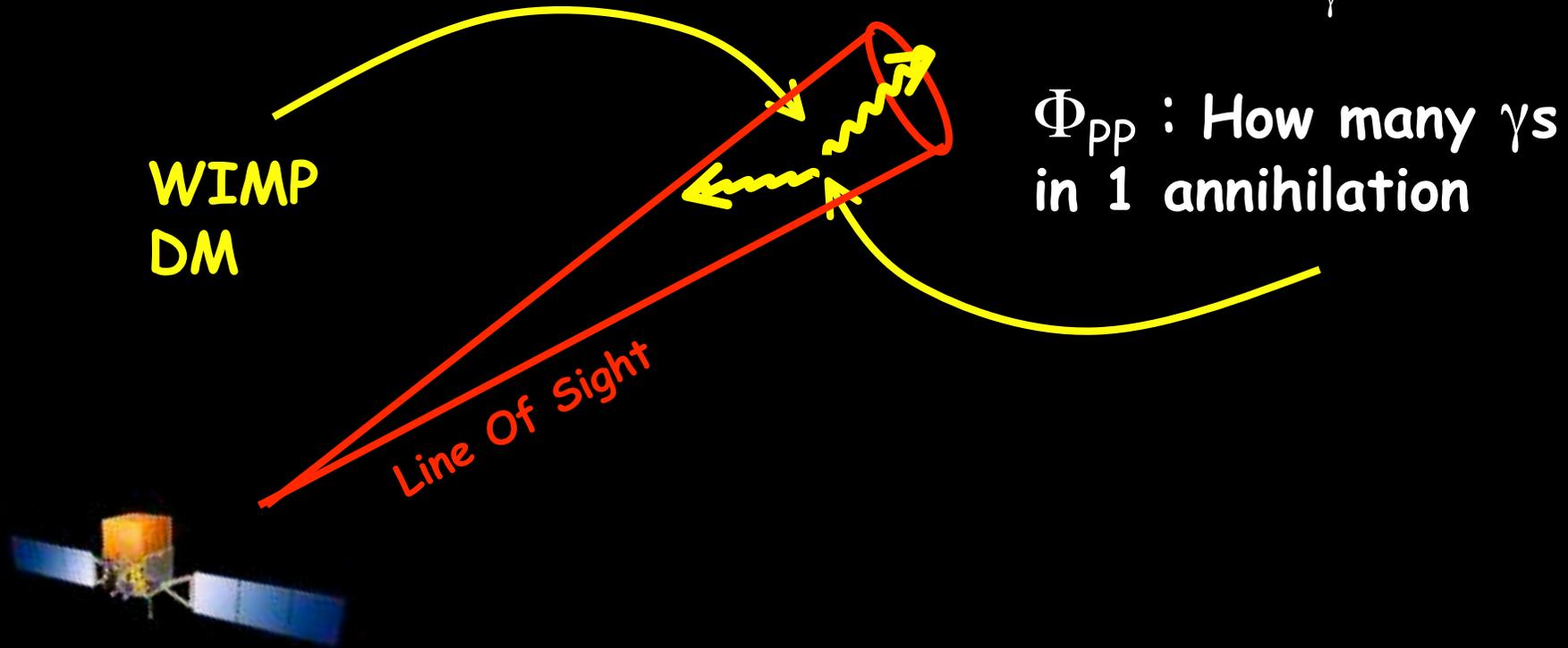


Bode et al, 2001

# DM structure is a fundamental ingredient for DM detection

i.e.  $\Phi_\gamma = \Phi_{\text{particle physics}} \times \Phi_{\text{cosmology}}$

$$\Phi_{\text{PP}} = \frac{1}{4\pi} \frac{\sigma_{\text{ann}} v}{2m_\chi^2} \int_{E_0}^{m_\chi} \sum_f \frac{dN_f^\gamma}{dE_\gamma} \text{BR}_f dE_\gamma$$



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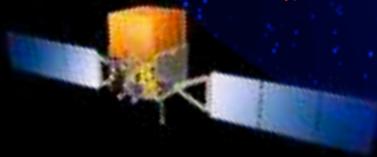
WIMP  
DM

$\Phi_{\text{PP}}$  : How many  $\gamma$ s  
in 1 annihilation

Line Of Sight

$$\Phi_{\text{cosmo}} = \int_{\Delta\Omega, \lambda} \frac{\rho_{\text{DM}}^2(r(\Delta\Omega, \lambda))}{\lambda^2} d\lambda d\Omega$$

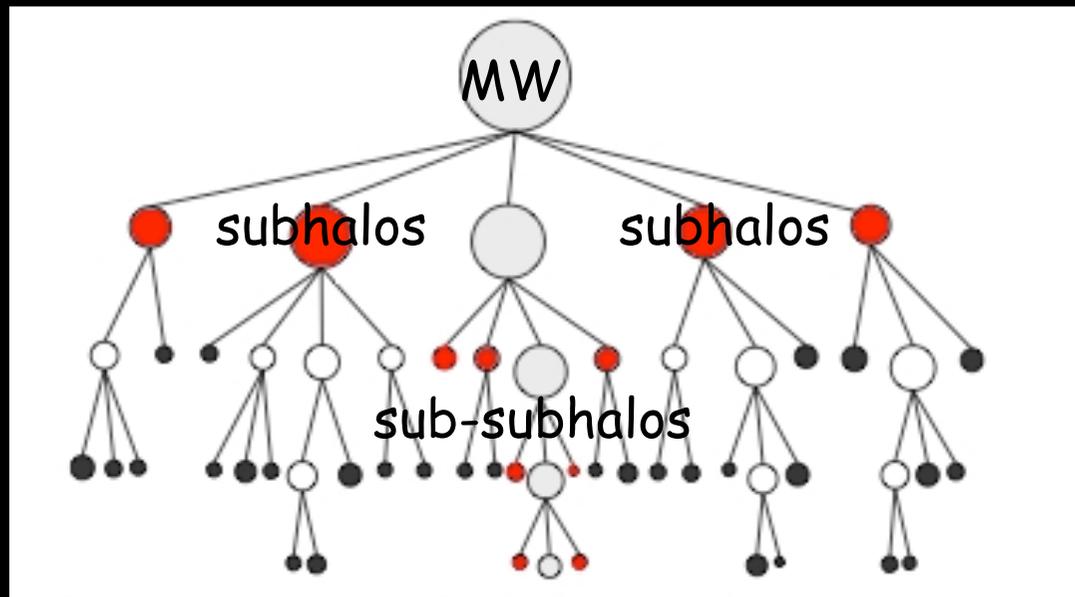
$\Phi_{\text{cosmo}}$  : How many annihilations  $\Leftrightarrow$   
How many and which sources



# Modeling the structure of dark matter halos

Halos form through a hierarchical process of successive mergers. The halo of our Galaxy will be self-similarly composed by:

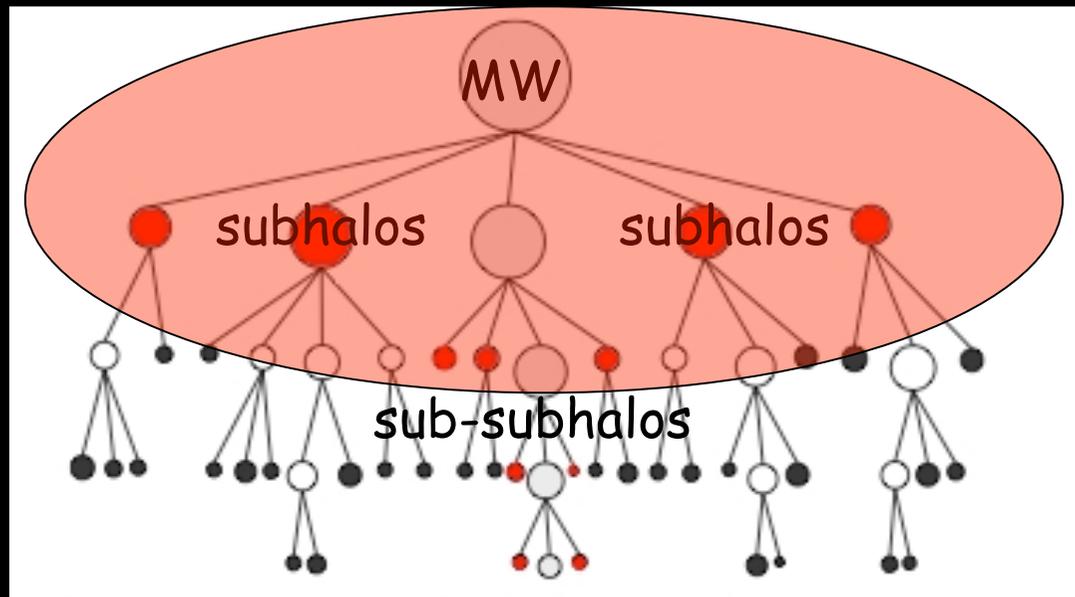
- a smoothly distributed component ( $\rho_{DM(h)}^2$  single halo )
- a number of virialized substructures ( $\rho_{DM(subh)}^2$  all halos)



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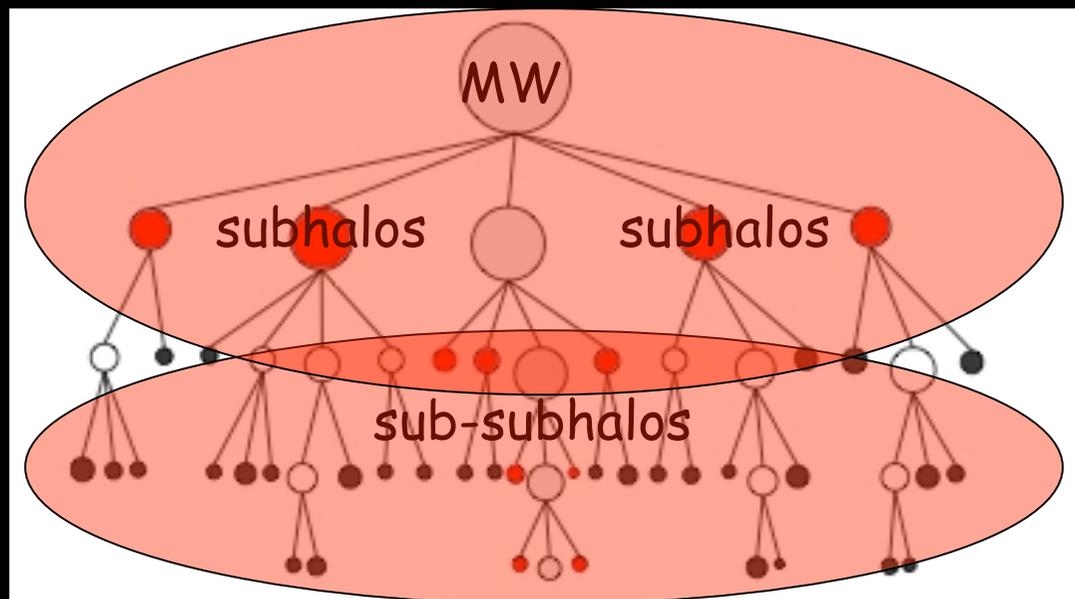


N-body simulations study the smooth halo and the larger halos ( $M > 10^5 M_{sun}$ ).

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Halos form through a hierarchical process of successive mergers. The halo of our Galaxy will be self-similarly composed by:

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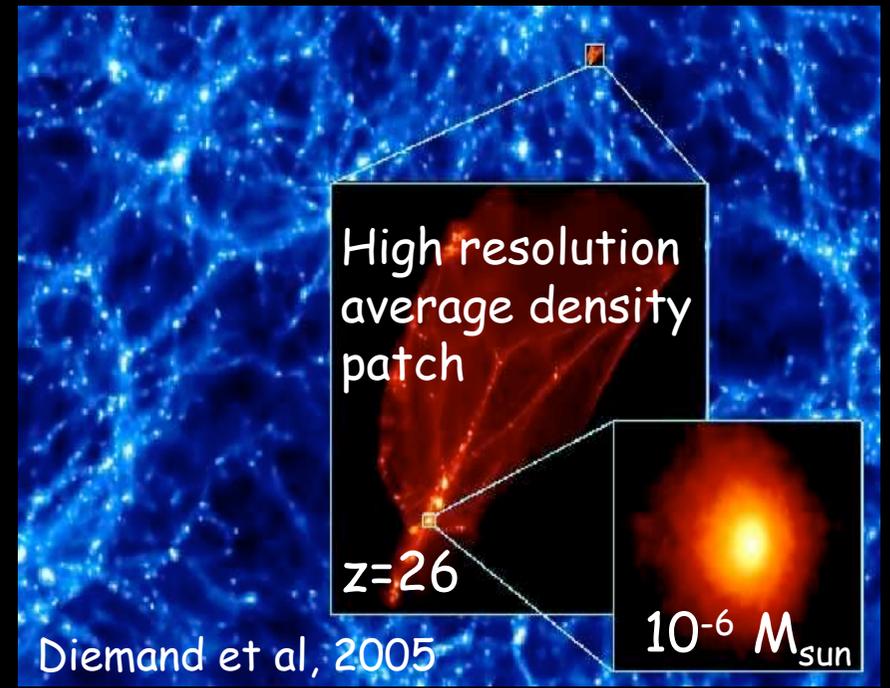
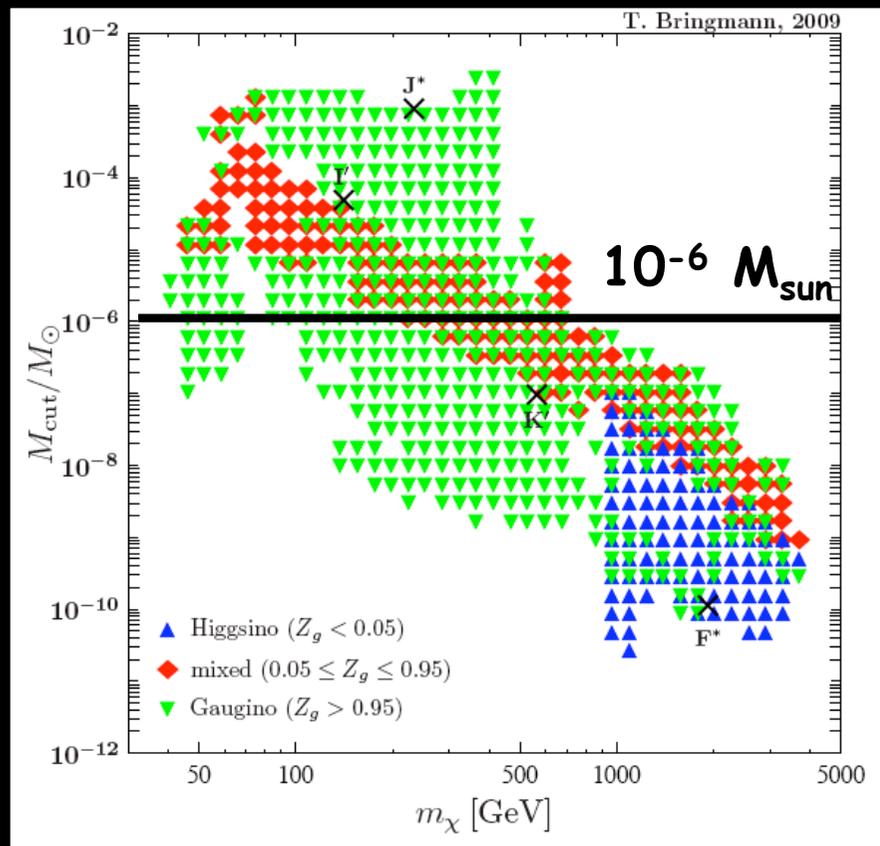
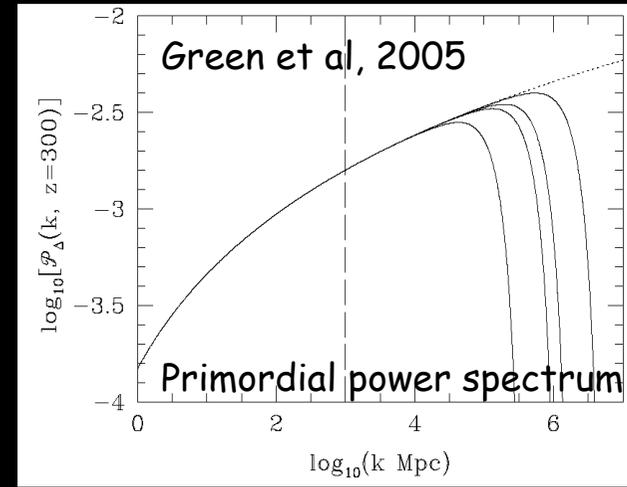
N-body simulations study the smooth halo and the larger halos ( $M > 10^5 M_{sun}$ ).

Microphysics and theory of structure formation sets the mass of the smallest halo because there is not enough CPU power to simulate small halos from collapse till today.

# Modeling the structure of dark matter halos from theory of structure formation ( $M < 10^5 M_{\text{sun}}$ )

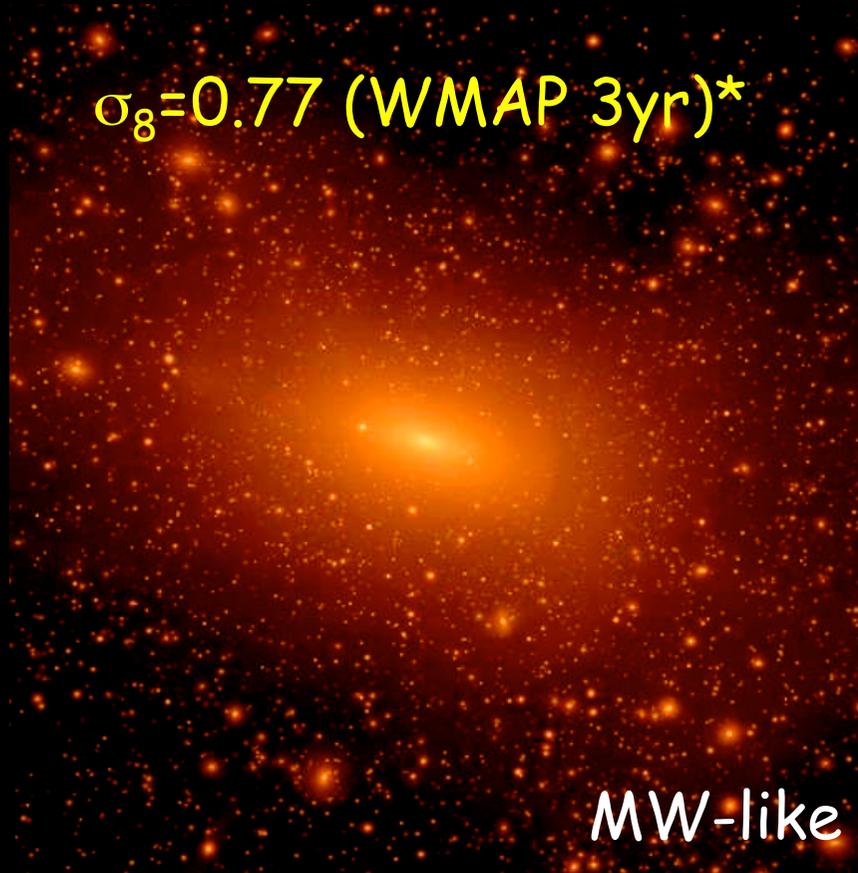
Theory: Damping of the primordial power spectrum due to CDM free streaming or acoustic oscillations after kinetic decoupling

Typical  $M_{\text{min}}$  for a WIMP =  $10^{-6} M_{\text{sun}}$



# Modeling the structure of dark matter halos from N-body simulations ( $M > 10^5 M_{\text{sun}}$ )

$\sigma_8 = 0.77$  (WMAP 3yr)\*

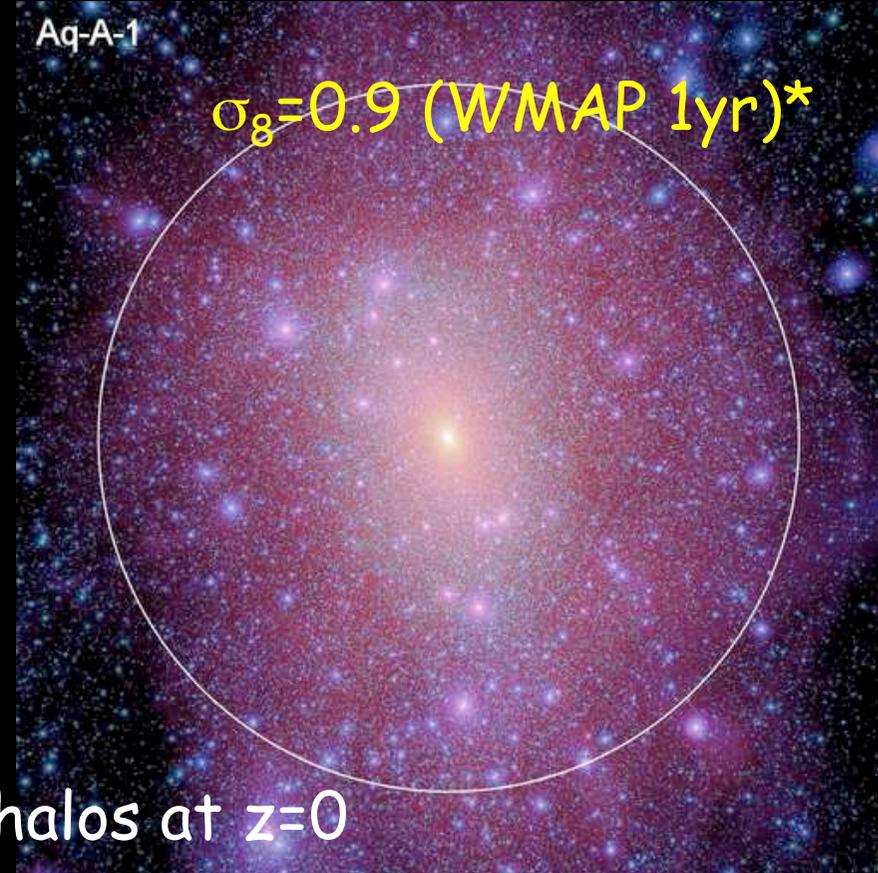


MW-like halos at  $z=0$

Via Lactea 2, Diemand et al

Aq-A-1

$\sigma_8 = 0.9$  (WMAP 1yr)\*

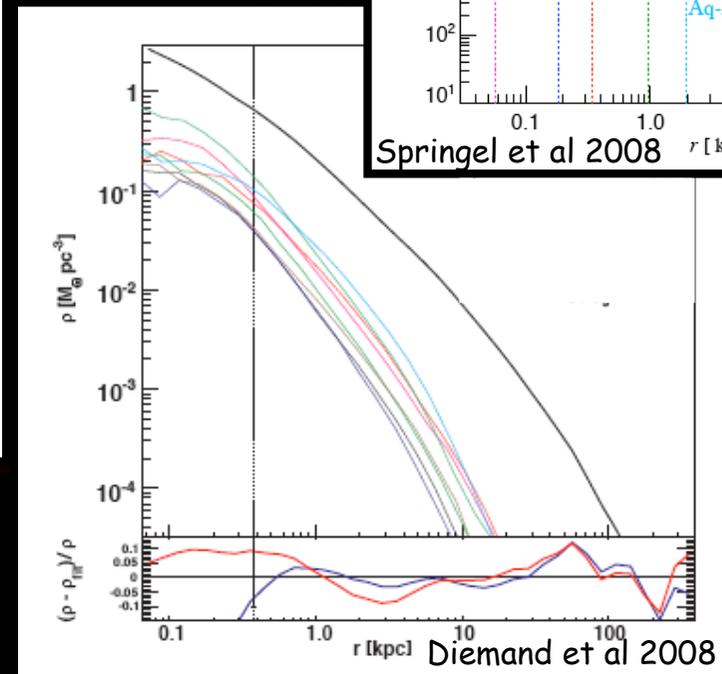
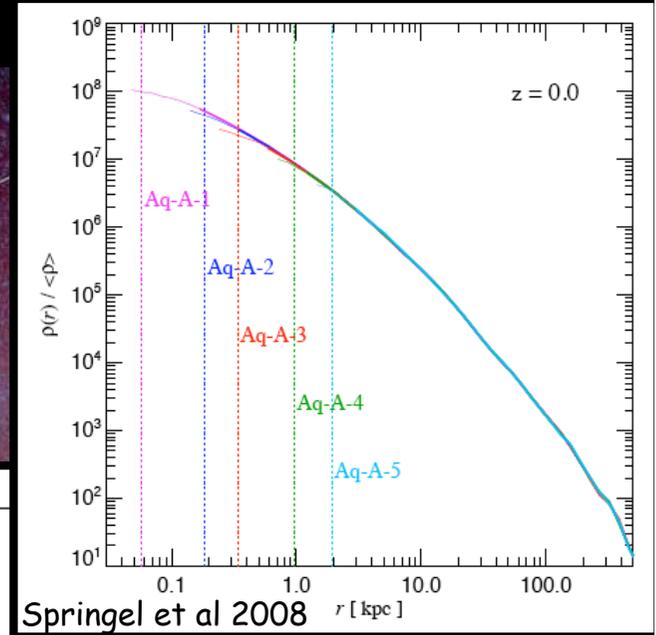
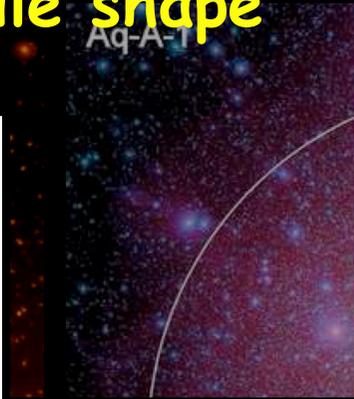
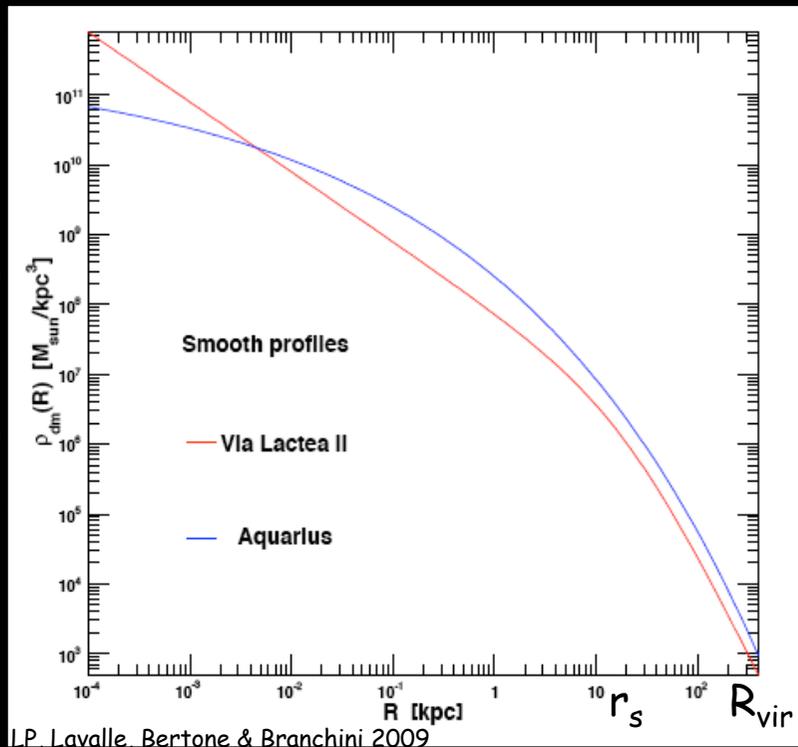


Aquarius, Springel et al

\*Note  $\sigma_8 = 0.8$  (WMAP 7yr)

# Modeling the structure of dark matter halos from N-body simulations ( $M > 10^5 M_{\text{sun}}$ )

→ Halo and subhalo profile shape



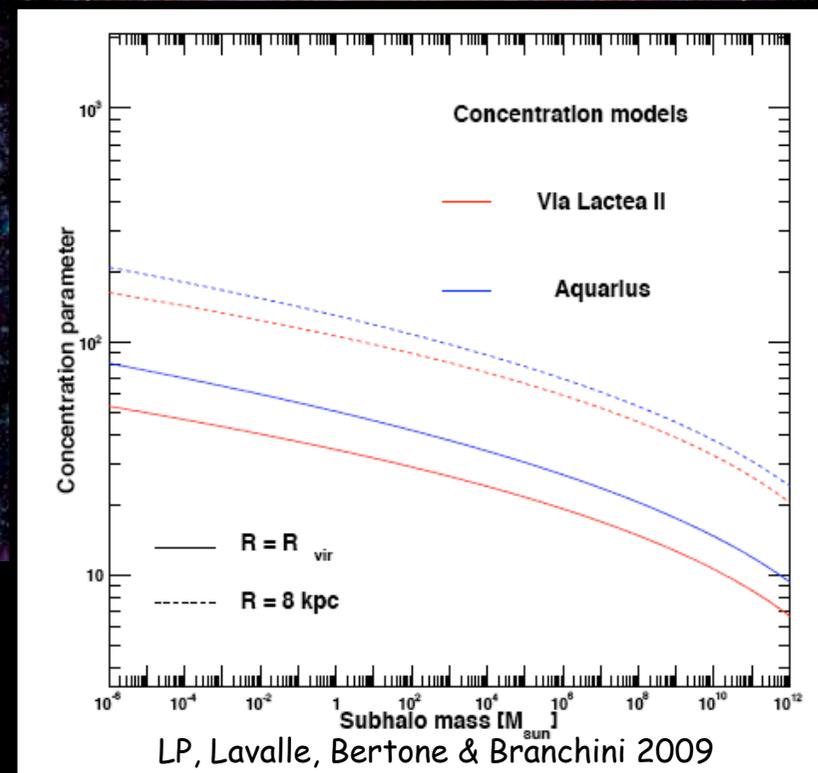
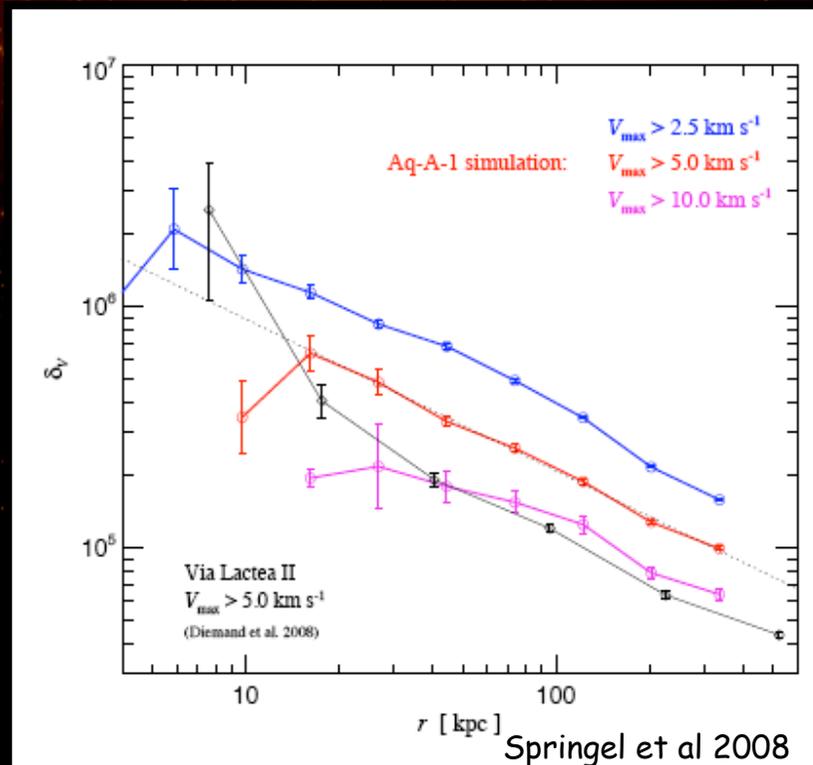
NFW VS Einasto

# Modeling the structure of dark matter halos from N-body simulations ( $M > 10^5 M_{\text{sun}}$ )

→ Halo and subhalo profile shape and concentration

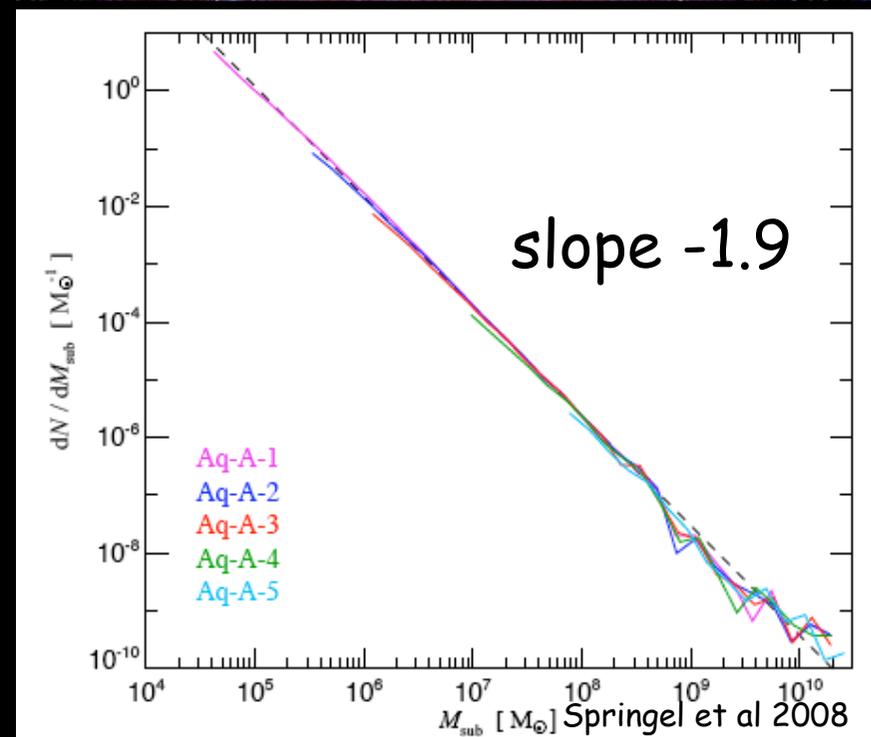
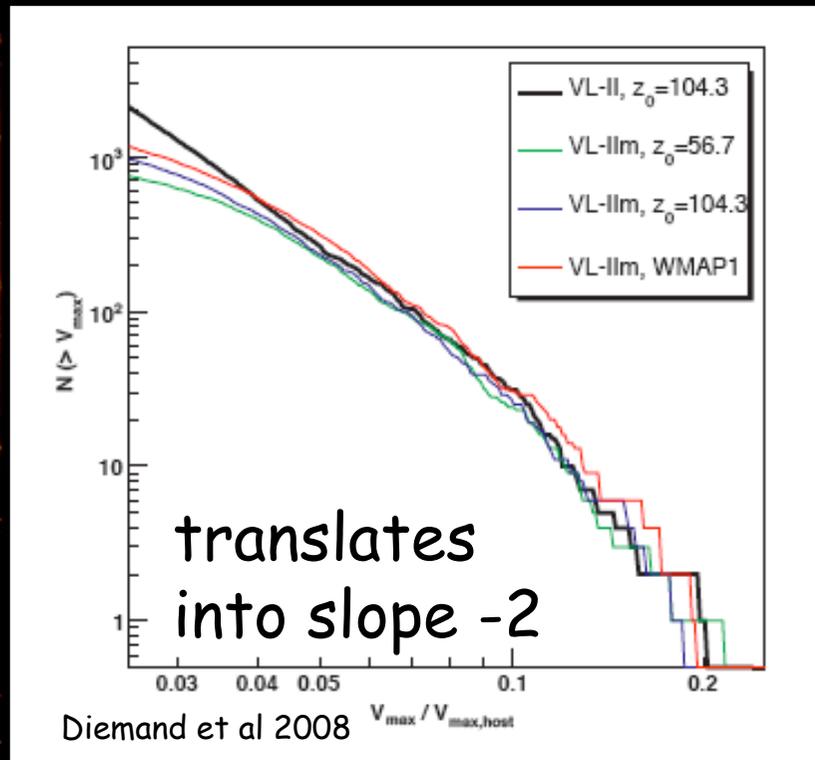
Concentration parameter differ (because of  $\sigma_8$ )

Concentration parameter ( $R_{\text{vir}}/r_s$ ) has radial dependence  
higher concentration → higher flux!



# Modeling the structure of dark matter halos from N-body simulations ( $M > 10^5 M_{\text{sun}}$ )

→ **Subhalo abundance and density distribution**



Note the different subhalo definition ( $v_{\text{max}}$  VS mass)

# Modeling the structure of dark matter halos from N-body simulations ( $M > 10^5 M_{\text{sun}}$ )

## → Subhalo abundance and density distribution

Mass slope  $\sim M^{-2}$

$$f_{\text{DM}} (>10^7 M_{\text{sun}}) \sim 11\%$$

$$f_{\text{DM}} (>10^{-6} M_{\text{sun}}) \sim 50\%$$

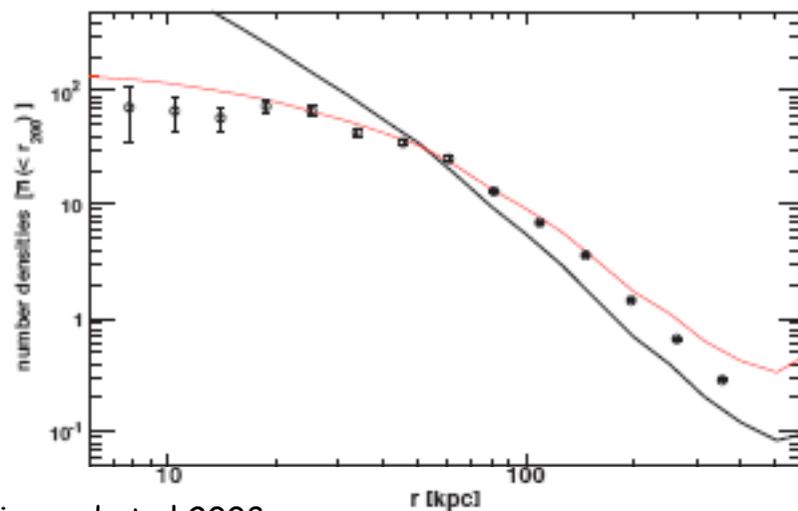
Radial distribution  $\sim (1+R/r_s)^{-1}$

Mass slope  $\sim M^{-1.9}$

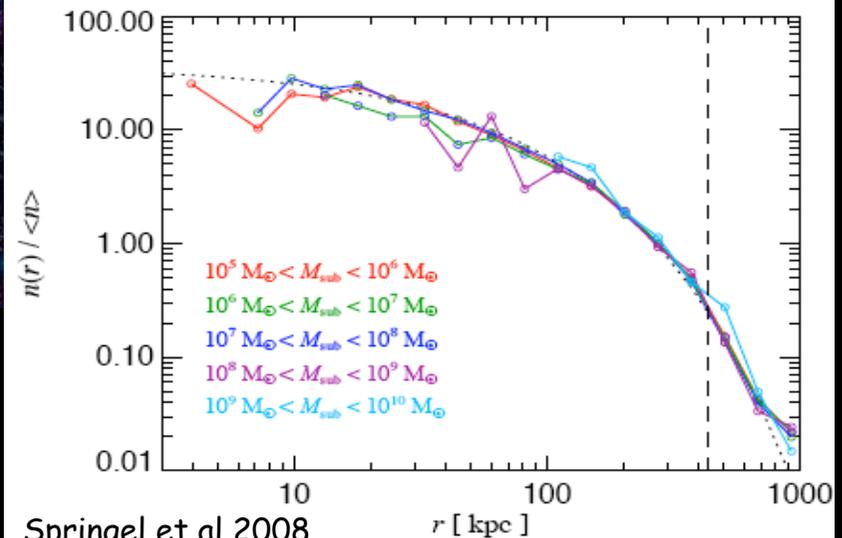
$$f_{\text{DM}} (>10^7 M_{\text{sun}}) \sim 13\%$$

$$f_{\text{DM}} (>10^{-6} M_{\text{sun}}) \sim 25\%$$

Radial distribution  $\sim \text{Einasto } \alpha=0.67$



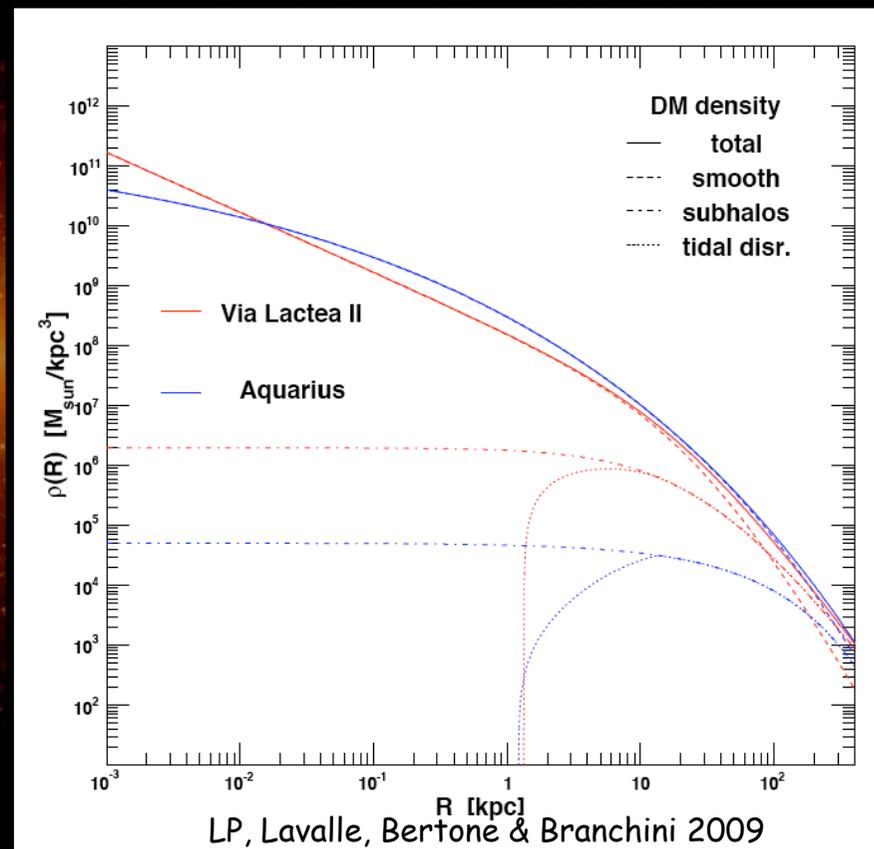
Diemand et al 2008



Springel et al 2008

# Modeling the structure of dark matter halos from N-body simulations ( $M > 10^5 M_{\text{sun}}$ )

→ **Subhalo abundance and density distribution**



**Roche criterion sets the effect of tidal forces**

# Predictions

$$\Phi_{\gamma} = \Phi_{\text{particle physics}} \times \Phi_{\text{cosmology}}$$

**Step 1: MW smooth and single subhalo contribution**

$$\Phi_{\text{COSMO}}^{\text{halo}}(M, R, r) \propto \int_{\text{l.o.s.}} d\lambda d\Omega \left[ \frac{\rho_{\text{DM}}^2(M, c(M, R), r, \psi)}{d^2} \right]$$

**Step 2: Integrated contribution of all the GALACTIC halos along the LOS**

$$\Phi^{\text{allhalos}}_{\text{COSMO}}(\psi, \Delta\Omega) \propto \int_M dM \int_c dc \iint_{\Delta\Omega} d\vartheta d\varphi \int_{\text{l.o.s.}} d\lambda \rho_{\text{sh}}(M, R) \cdot P(c) \Phi_{\text{COSMO}}^{\text{halo}}$$

# Predictions

$$\Phi_\gamma = \Phi_{\text{particle physics}} \times \Phi_{\text{cosmology}}$$

## Step 3: Integrated contribution of EXTRAGALACTIC halos and subhalos

Computing the cosmological  $\gamma$ -ray flux due to DM annihilation in halos...

$$\frac{d\phi_\gamma}{dE_0} = \frac{\sigma v}{8\pi} \frac{c}{H_0} \frac{\bar{\rho}_0^2}{m_\chi^2} \int dz (1+z)^3 \frac{\Delta^2(z)}{h(z)} \frac{dN_\gamma(E_0(1+z))}{dE} e^{-\tau(z, E_0)}$$

Enhancement due to halo weighted for the halo mass function  $\propto \frac{d \log N}{d \log M} \Delta_M^2$   
 ... and subhalos...

$$M \Delta_M^2 \rightarrow \int_{M_{\min}} dM_{\text{sub}} \int_0^{R_{\text{vir}}(M)} 4\pi R^2 dR \int dc P(c) M_{\text{sub}} \rho_{\text{sh}}(M_{\text{sub}}, M, R) c(M_{\text{sub}}, R)^3 \frac{I_2(c)}{I_1^2(c)}$$

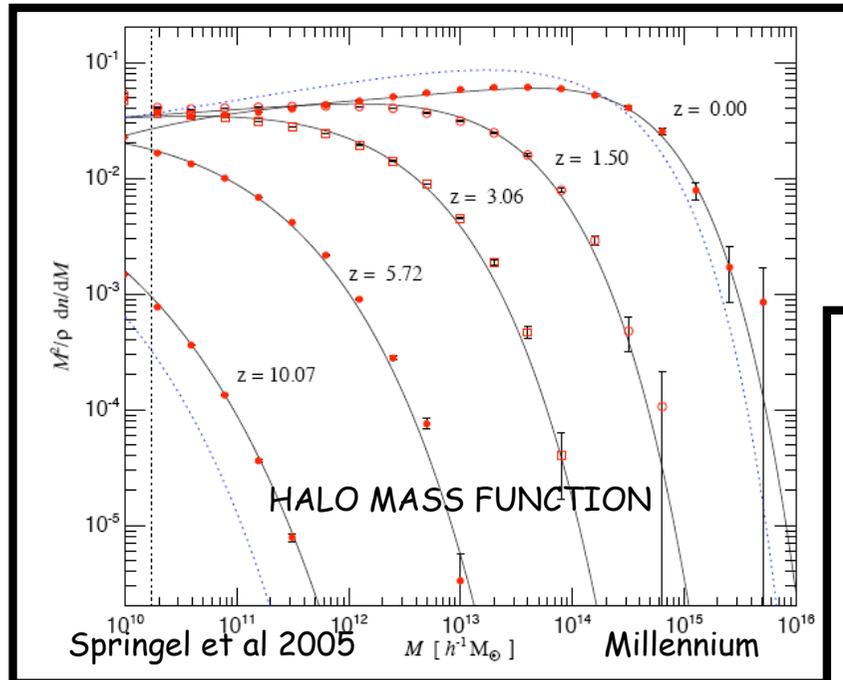
Normalized to subhalo mass fraction  $f(M)$

$$\propto \int_{\text{LOS}} \rho_{\text{sub}}^2(M_{\text{sub}})$$

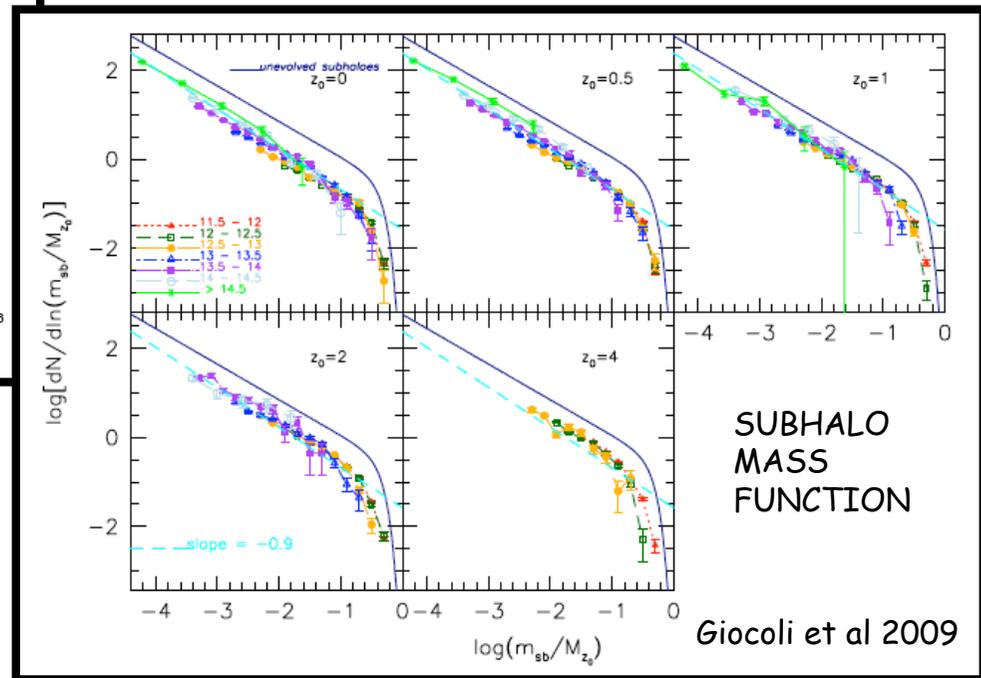
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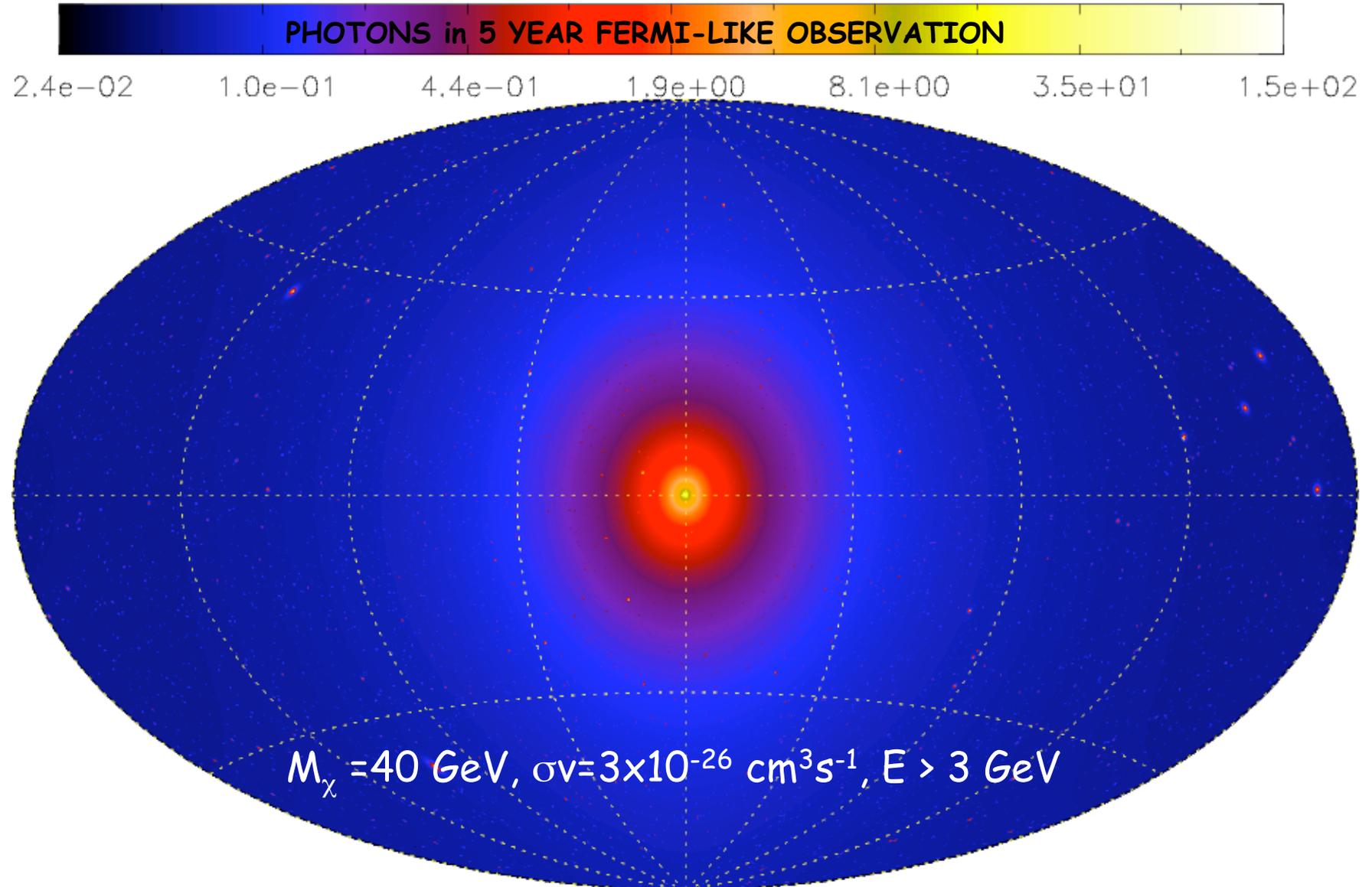


Mass function as predicted by TSF is found in N-body

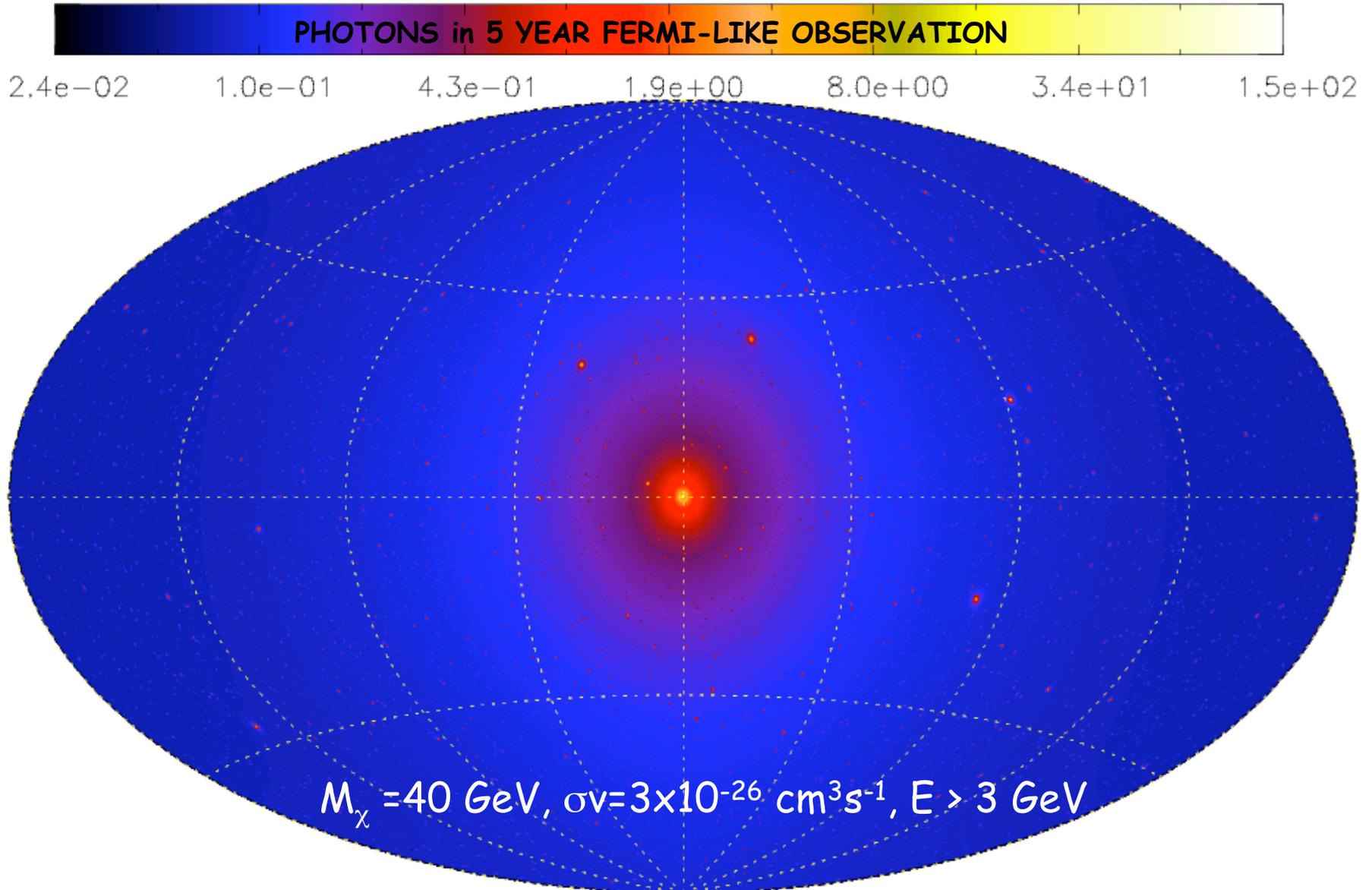


# The $\gamma$ -ray sky (Aquarius)

## Galactic and extragalactic: smooth + subhalos

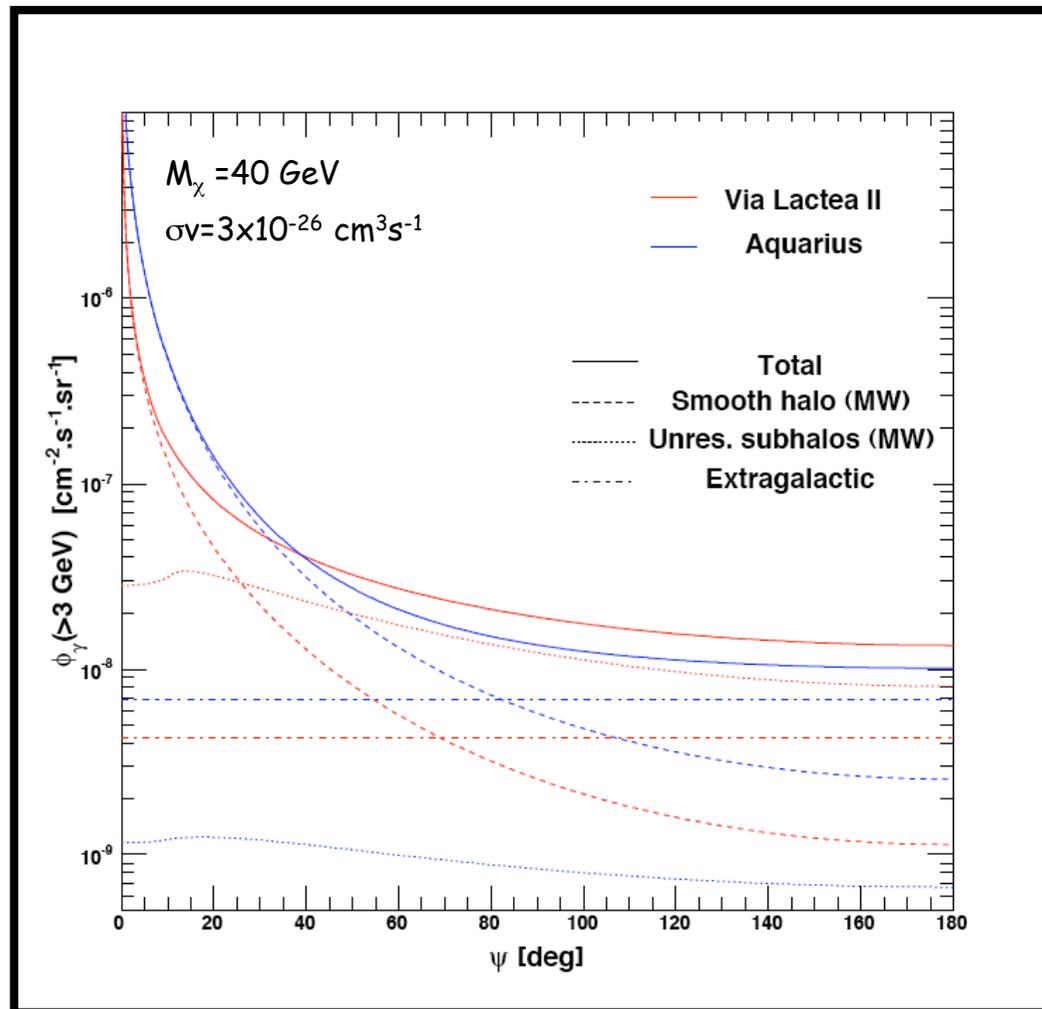


# The $\gamma$ -ray sky (Via Lactea 2) Galactic and extragalactic: smooth + subhalos

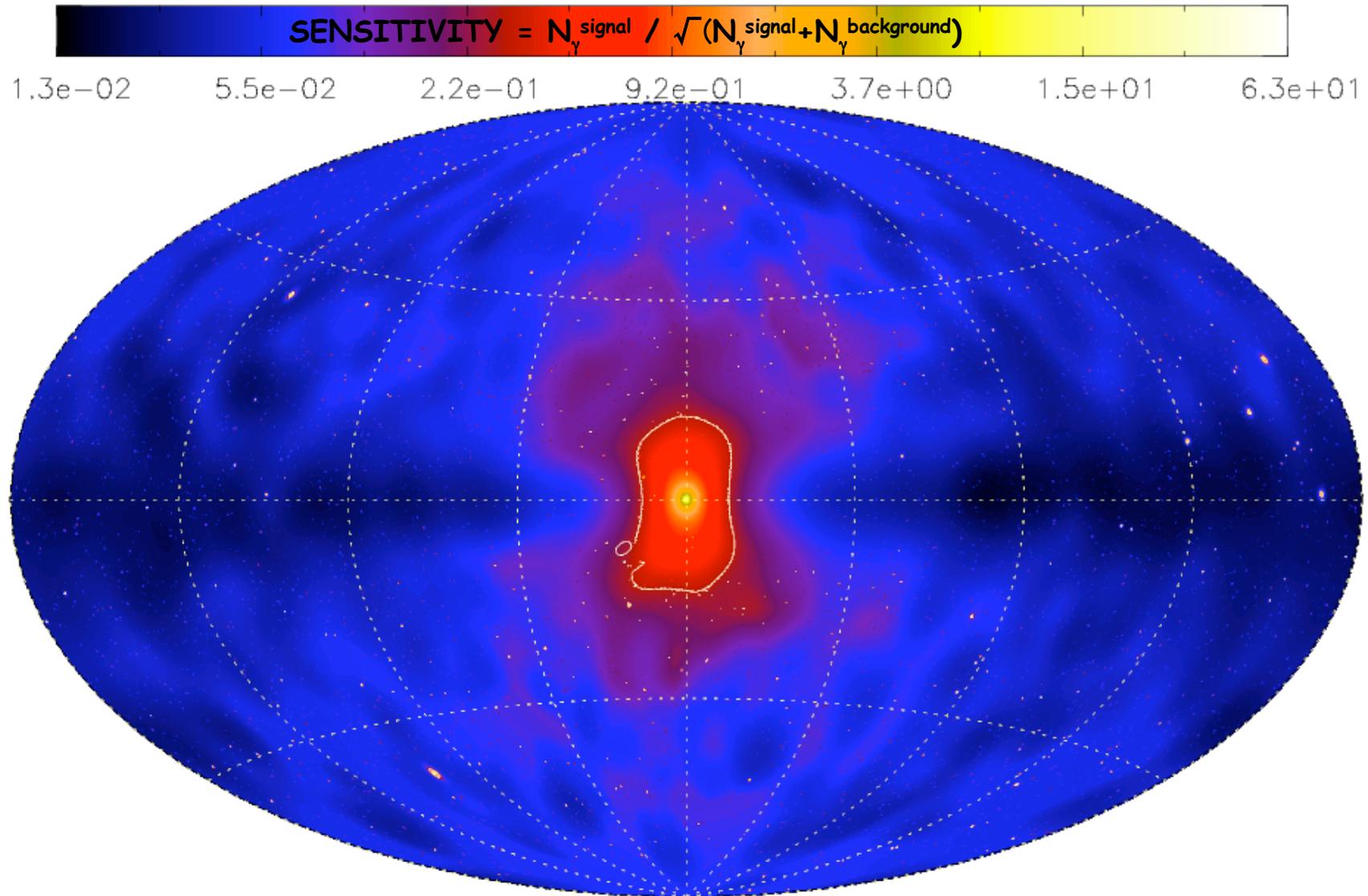


# The $\gamma$ -ray sky

## Galactic and extragalactic: smooth + clumpy



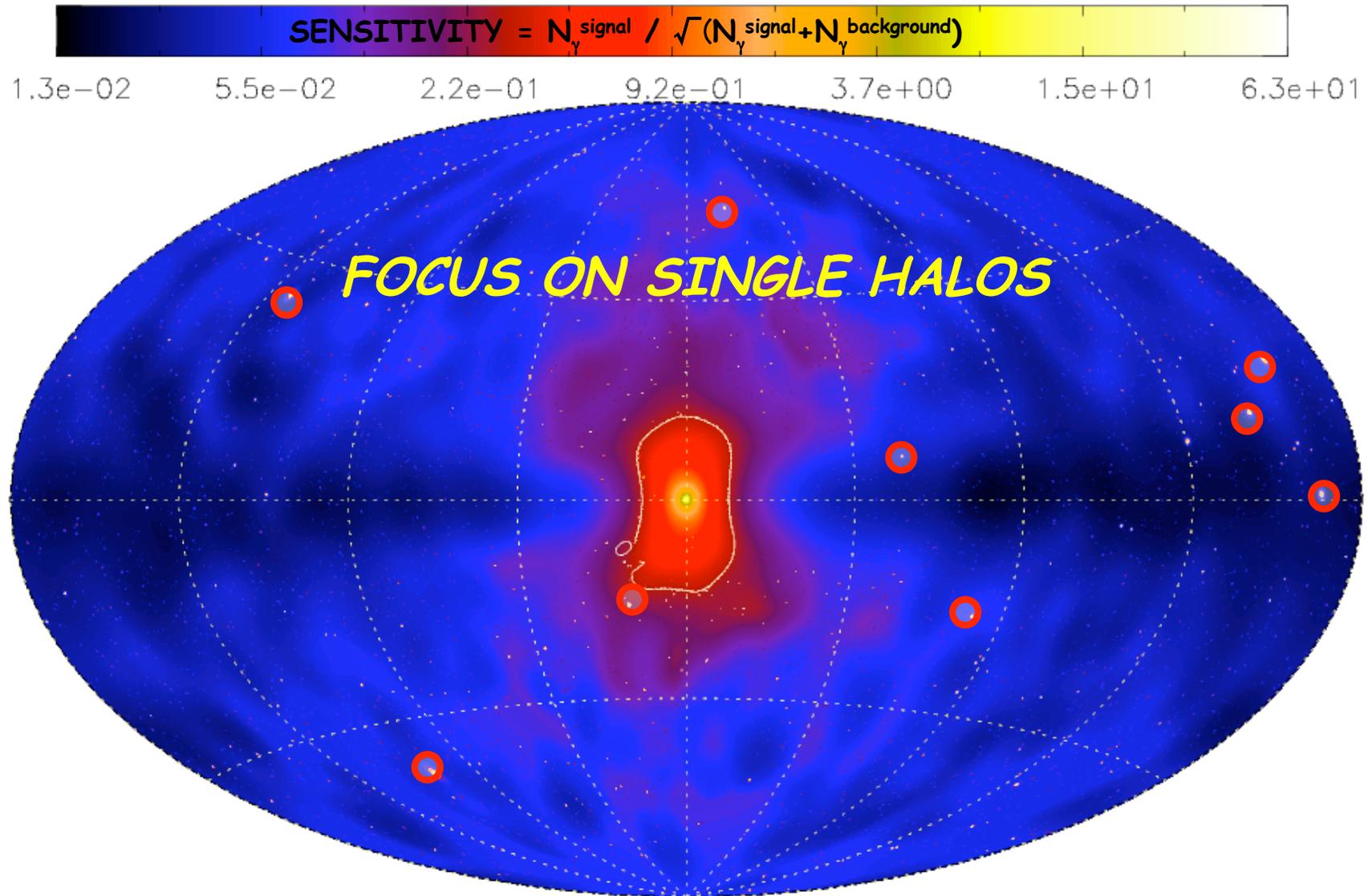
# Is the $\gamma$ -ray sky from DM annihilation DETECTABLE?



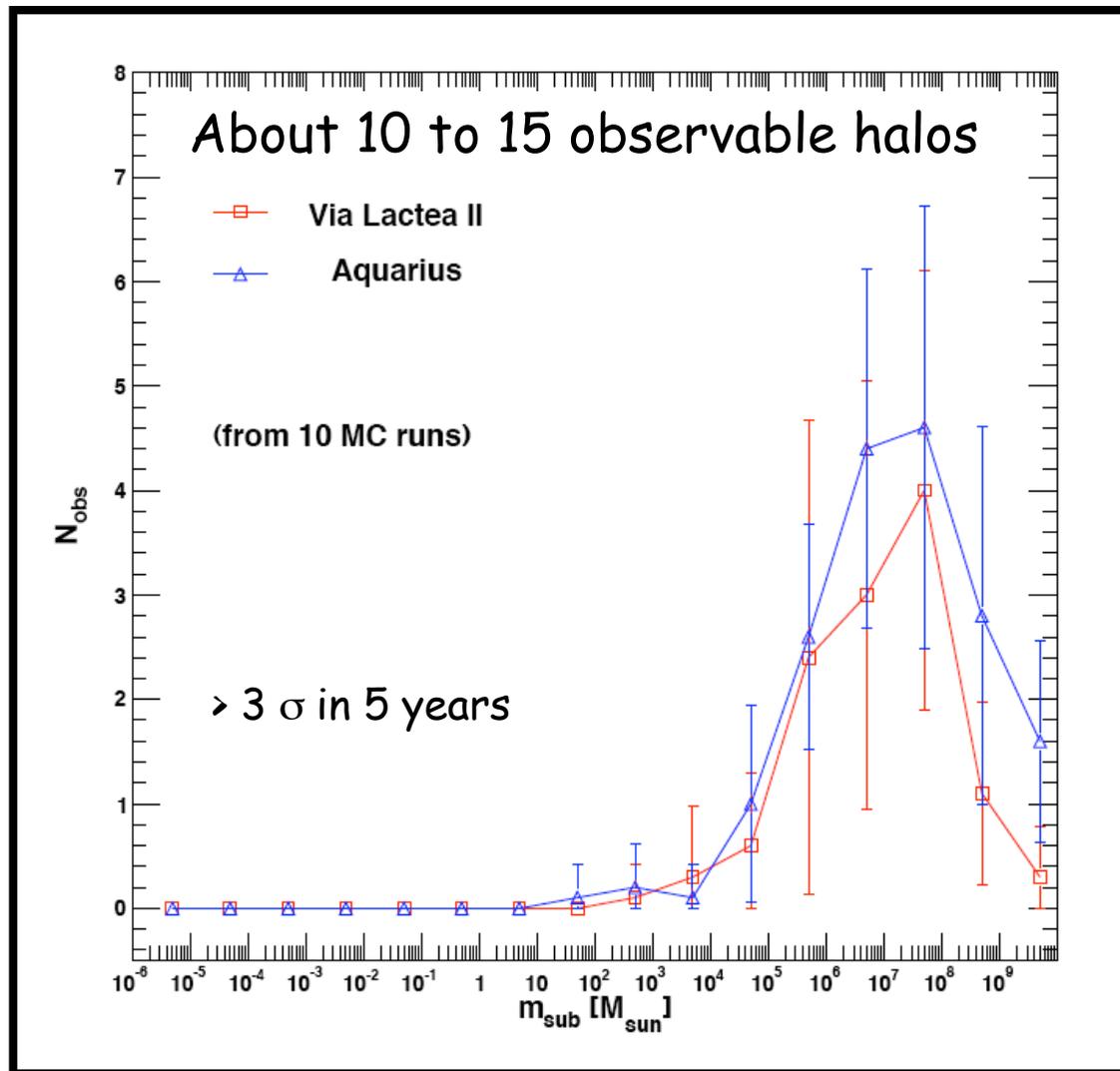
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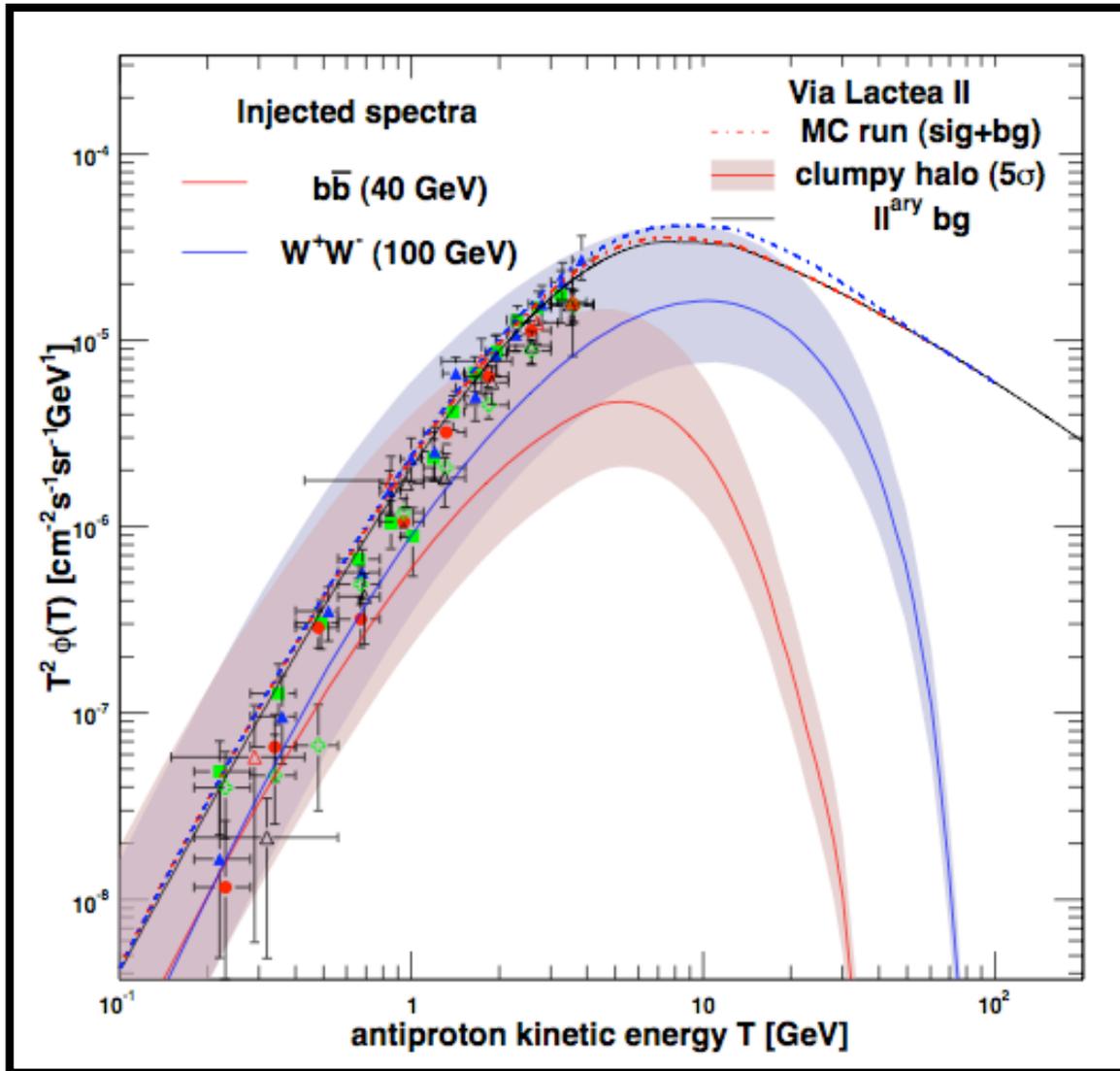
# Is the $\gamma$ -ray sky from DM annihilation DETECTABLE?



# Is the $\gamma$ -ray sky from DM annihilation DETECTABLE?



Check with the antiproton flux deriving from observable subhalos.. And it is OK..



This is an example of combining multi-messenger results in order to get stable predictions or exclude particle models

See, e.g., Pato, LP & Bertone 2009  
Catena, Fornengo, Pato, LP & Masiero 2010  
Colafrancesco, Lieu, Marchegiani, Pato & LP 2010

to appear in LP, Lavallo, Bertone & Branchini 2009 - revised

# Beyond the first monopole angular correlations on the diffuse $\gamma$ -ray background

INGREDIENTS:

Take the  $\gamma$ -ray flux due to DM annihilation in the galactic subhalos

**AND**

the cosmological  $\gamma$ -ray flux due to DM annihilation

$$\frac{d\phi_\gamma}{dE_0} = \frac{\sigma v}{8\pi} \frac{c}{H_0} \frac{\bar{\rho}_0^2}{m_\chi^2} \int dz (1+z)^3 \frac{\Delta^2(z)}{h(z)} \frac{dN_\gamma(E_0(1+z))}{dE} e^{-\tau(z, E_0)}$$

and compute the coefficients of the decomposition in spherical harmonics

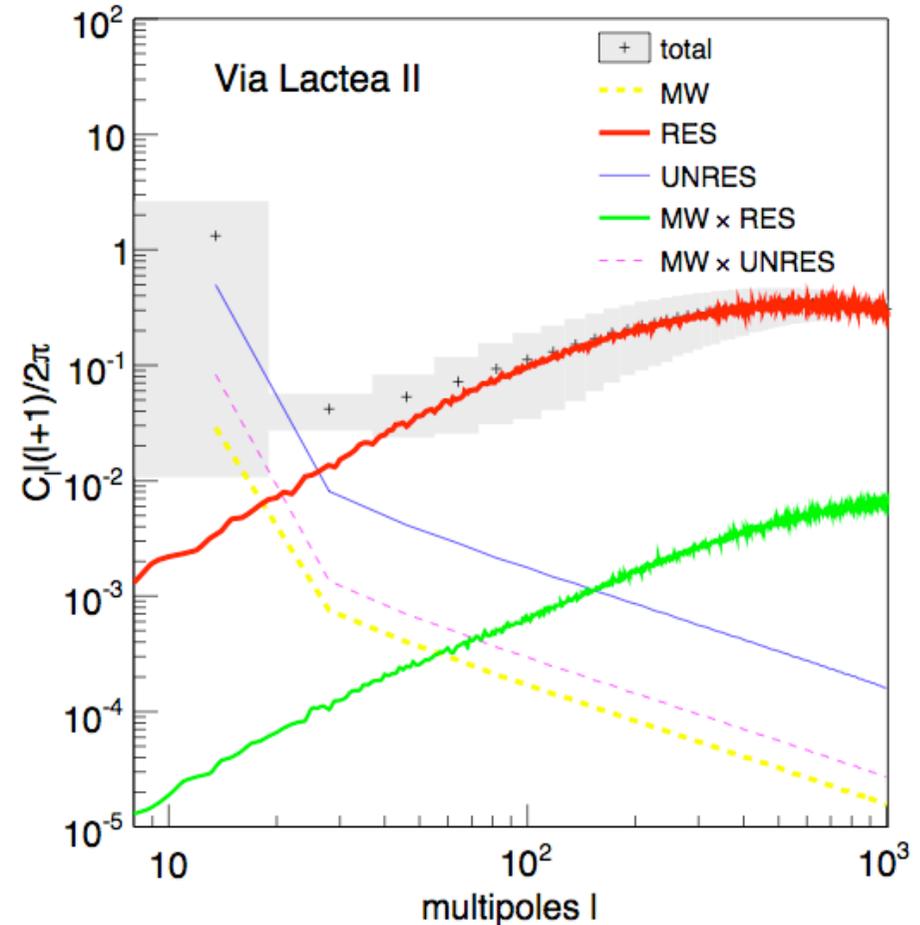
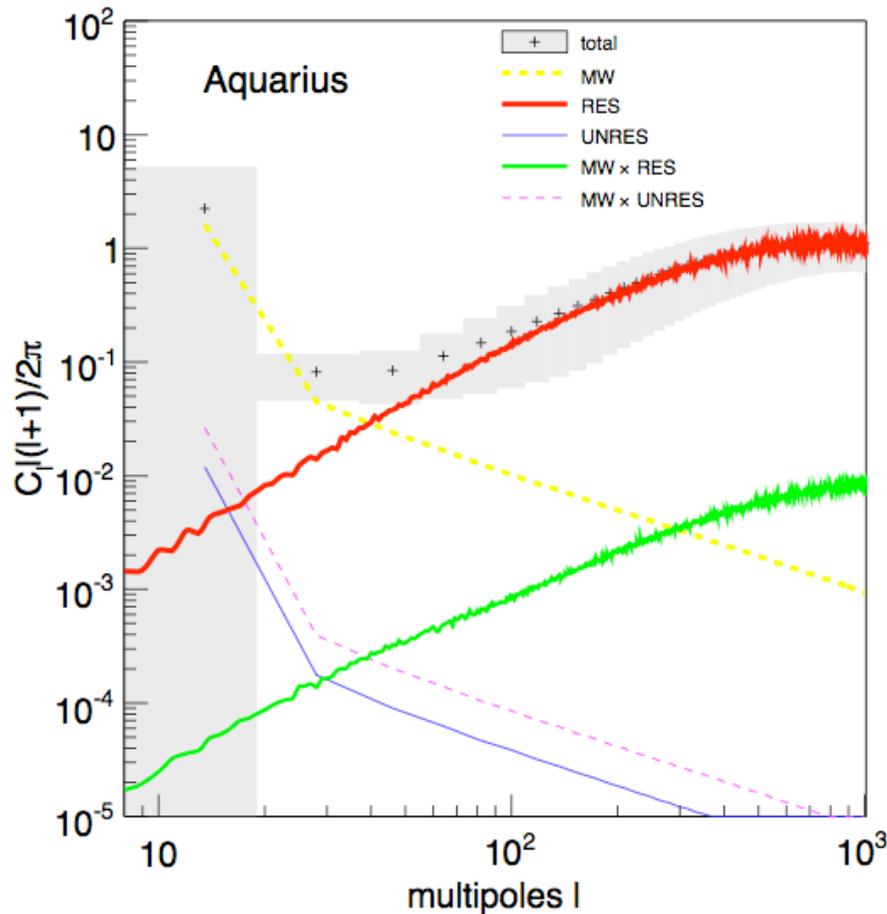
$$\left\langle \frac{d\phi}{dE d\Omega} \right\rangle a_{l,m} = \int d\Omega \left( \frac{d\phi}{dE d\Omega} - \left\langle \frac{d\phi}{dE d\Omega} \right\rangle \right) Y_{l,m}(\theta, \varphi)^*$$

$$c_l = \frac{\sum_{m=0}^l |a_{l,m}|^2}{2l+1}$$

# Angular correlations on the diffuse $\gamma$ -ray background

## Galactic subhalos

-checked against different number of simulated Galactic subhalos-



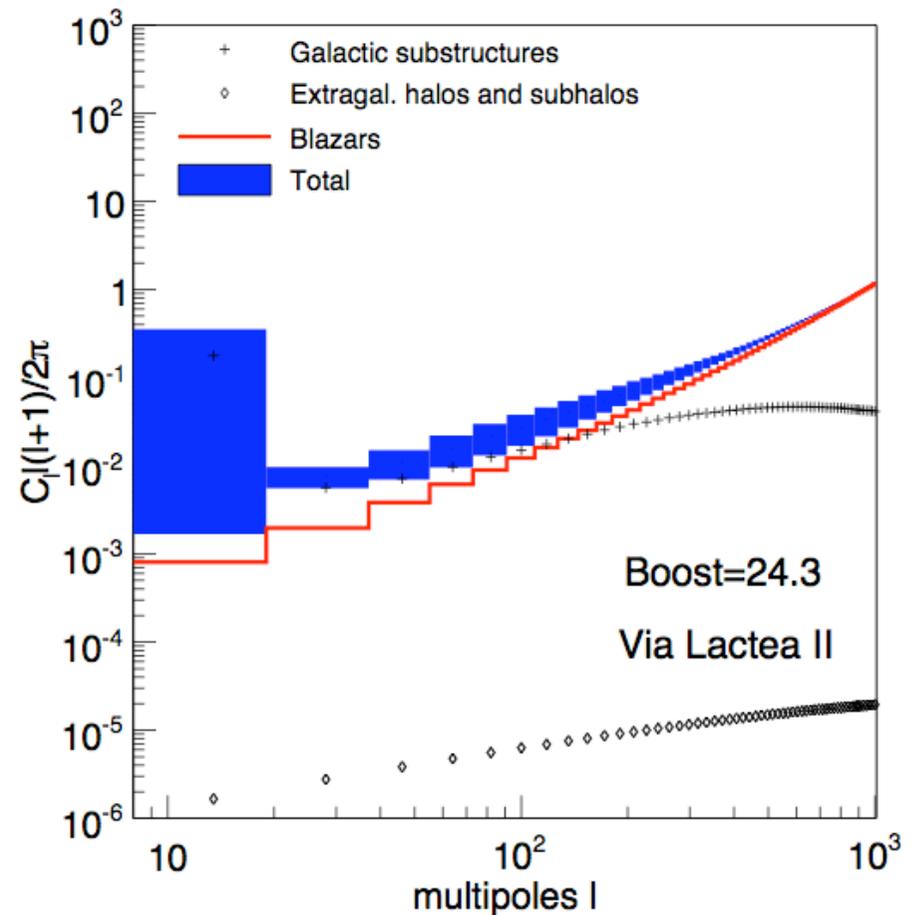
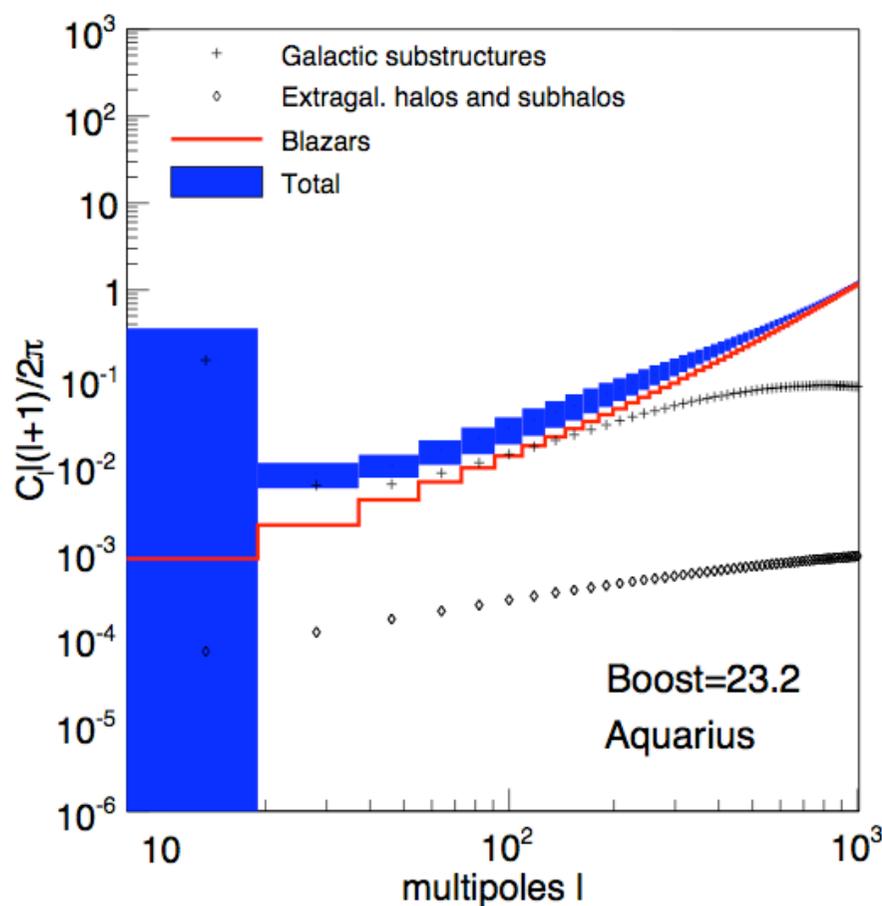
$$M_\chi = 40 \text{ GeV}, \sigma v = 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}, E = 10 \text{ GeV}$$

Ando, Bertone, Branchini, Fornasa, LP *in preparation*

# Angular correlations on the diffuse $\gamma$ -ray background (toy model: assume EGB = 60% EGRET EGB)

## Comparison with EGB à la Ando&Komatsu

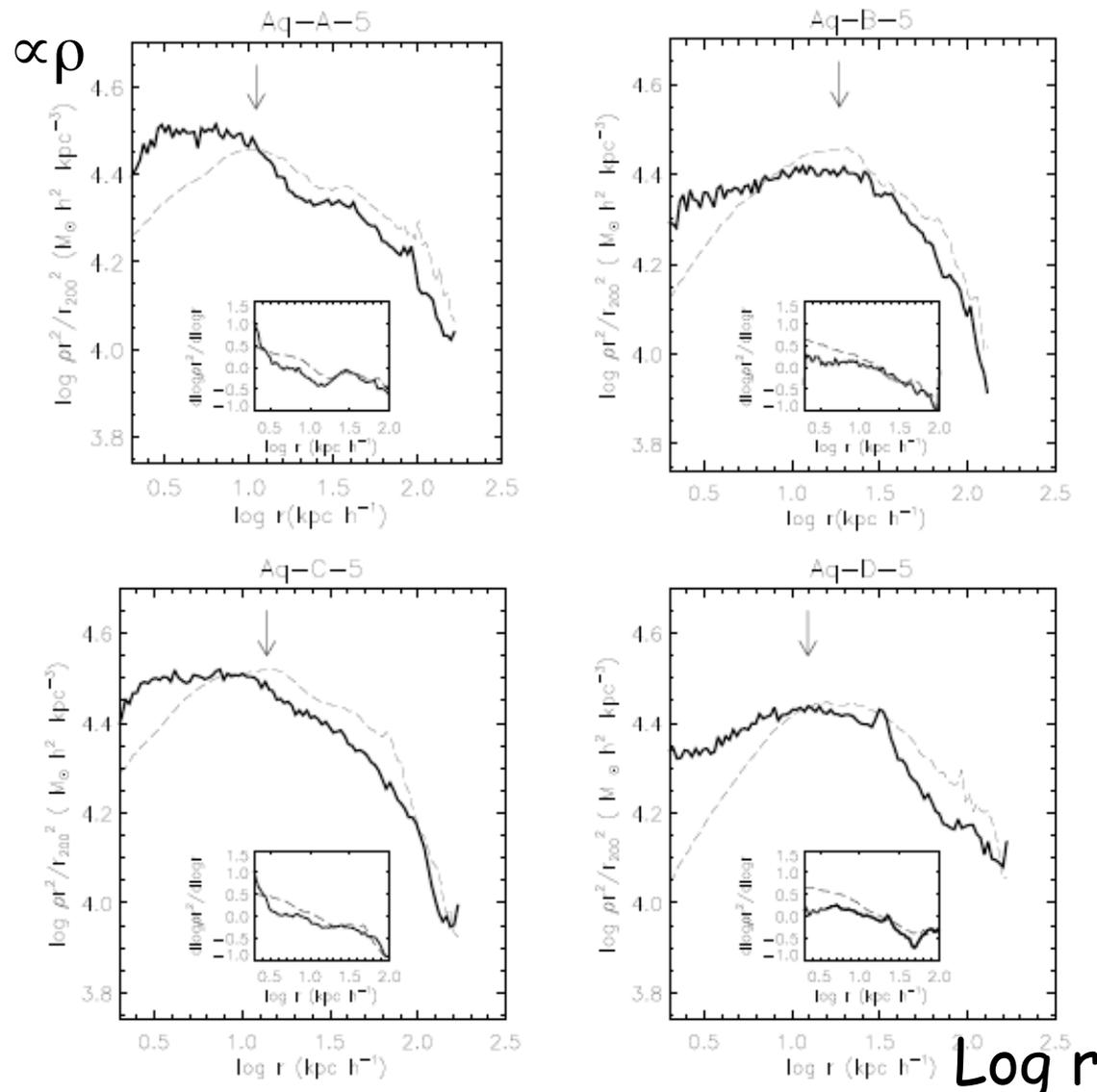
-we take the shape for blazar and extragalactic DM from them-



$M_\chi = 40 \text{ GeV}$ ,  $\sigma v = 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$  boosted to be 60% of EGB,  $E = 10 \text{ GeV}$

Ando, Bertone, Branchini, Fornasa, LP in preparation

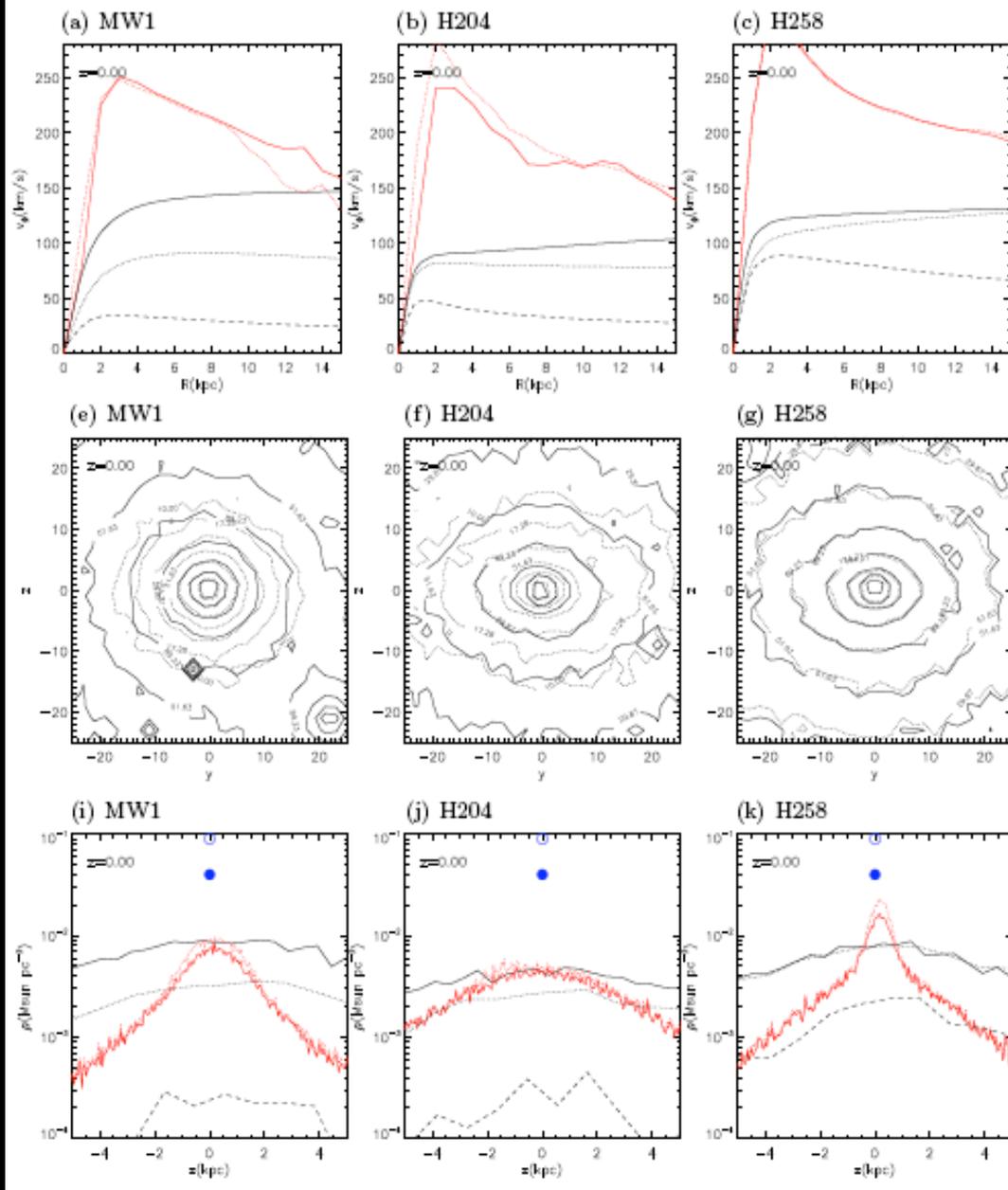
# The frontier : simulations including baryons



Tissera et al. 2009  
resimulated 6 Aquarius  
MW-like halos including  
metal-dependent cooling,  
star formation and  
supernova feedback  
**Found steeper DM profiles**  
Specific results depend on  
merging history

Agertz et al 2010  
(Ben Moore group)  
are producing high  
resolution  
simulations of the MW  
including baryons..  
**Stay tuned (Agertz, Bertone,  
Pato, LP, Diemand, Moore, 2010)**

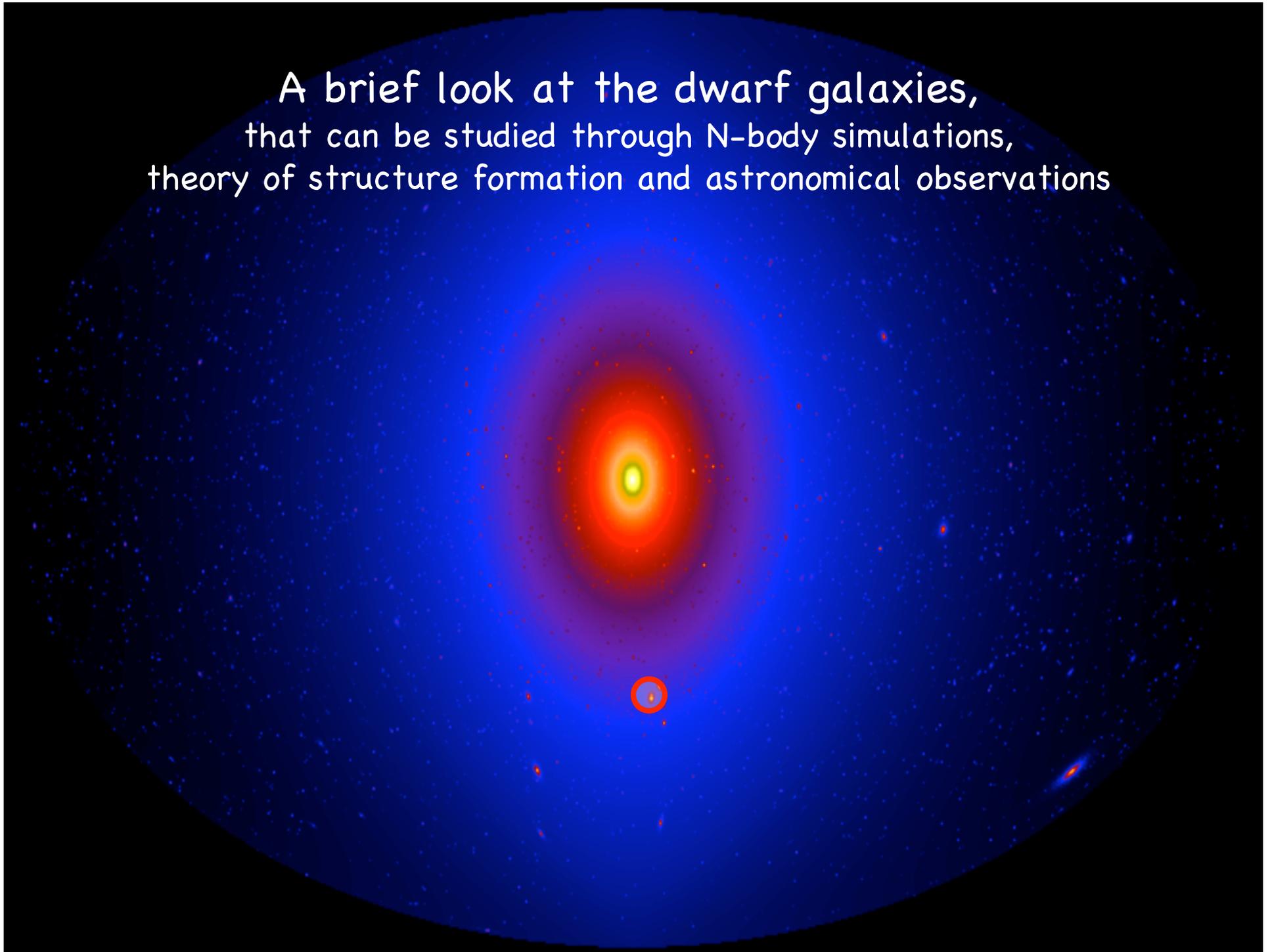
## The case : the dark disc



Read et al. 2009 found that baryons in the disk causes merging satellites to be dragged towards the disk and be torn apart, resulting in a dark matter disk, which gives anisotropic DM velocity distribution at the solar neighbourhood with interesting implications on WIMP capture and annual modulation signal.

Specific results depend on merging history

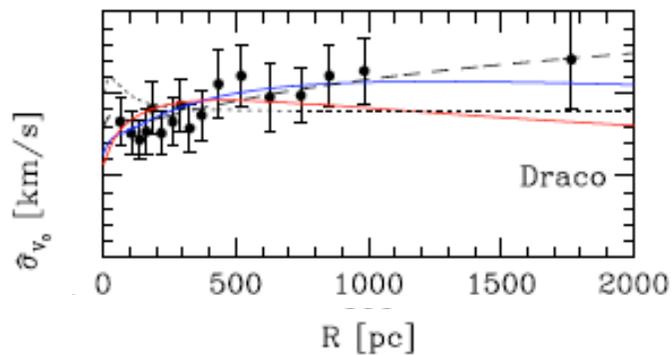
A brief look at the dwarf galaxies,  
that can be studied through N-body simulations,  
theory of structure formation and astronomical observations



Dwarf galaxies are the only objects whose density profiles are nicely inferred by astronomical measurements

-> small astrophysical uncertainty

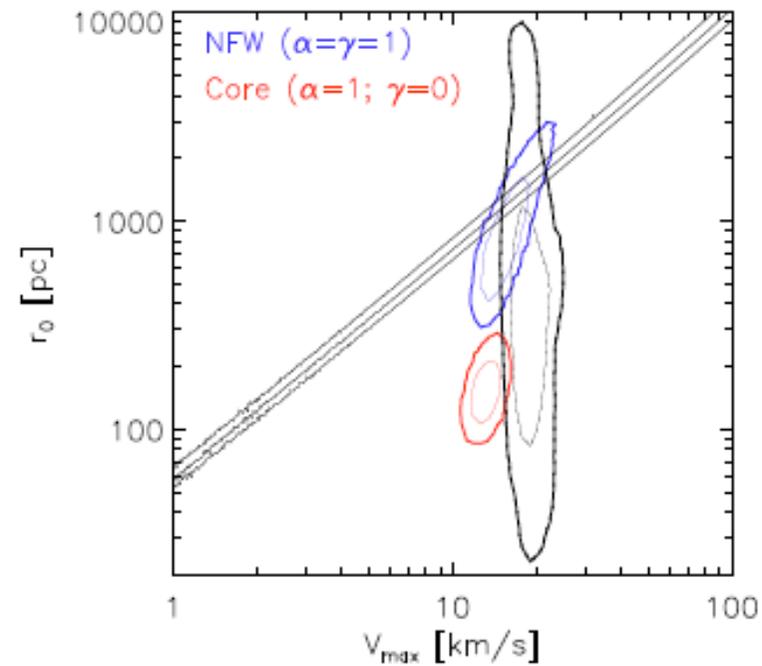
from velocity dispersions..



... to density profiles.

Universal behaviour!

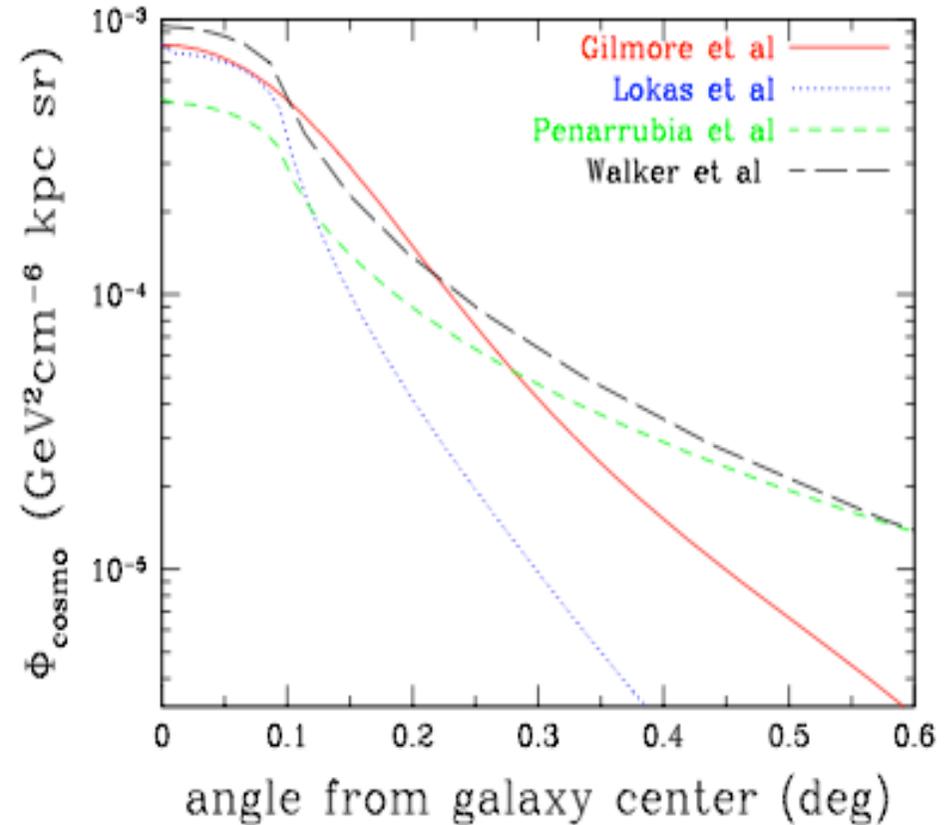
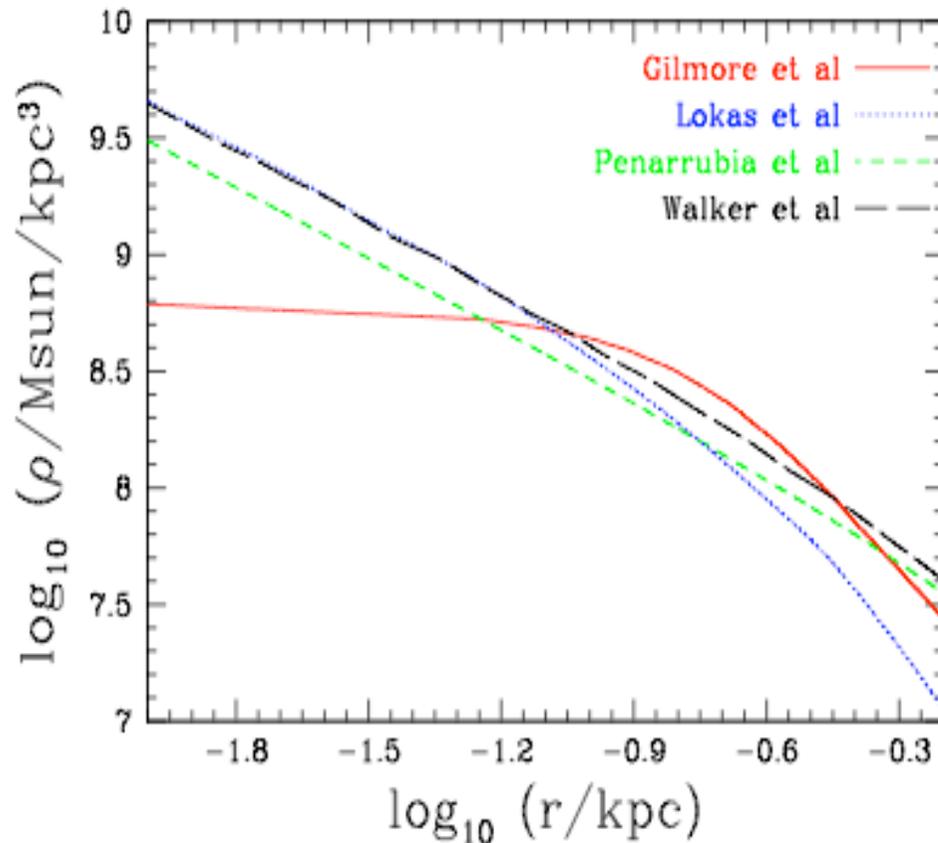
NFW preferred by  $\chi^2$  analysis



Walker et al, 2009

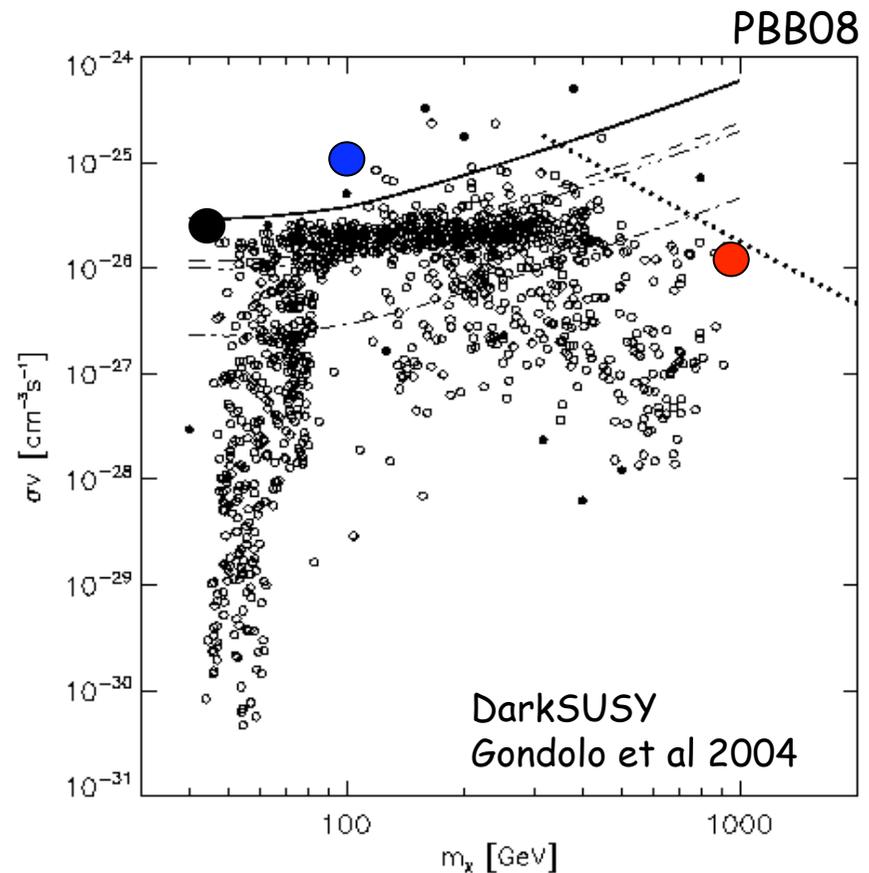
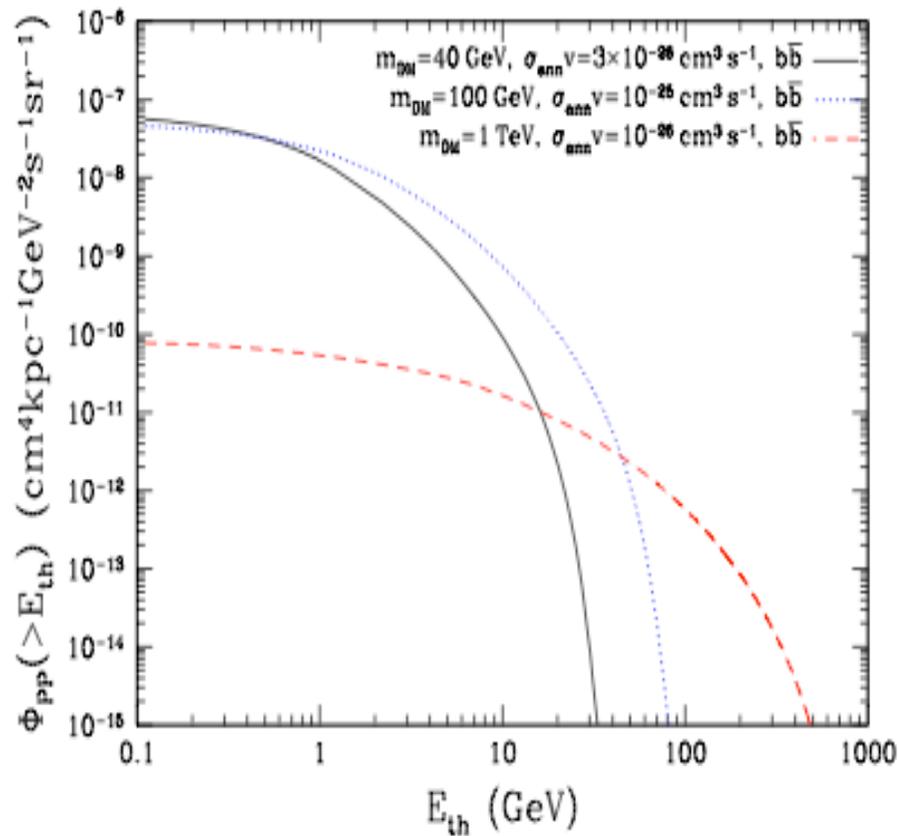
Computing  $\Phi_\gamma = \Phi_{\text{particle physics}} \times \Phi_{\text{cosmology}}$

$$\Phi_{\text{cosmo}} = \int_{\Delta\Omega, \lambda} \frac{\rho^2(r(\Delta\Omega, \lambda))}{\lambda^2} dV$$



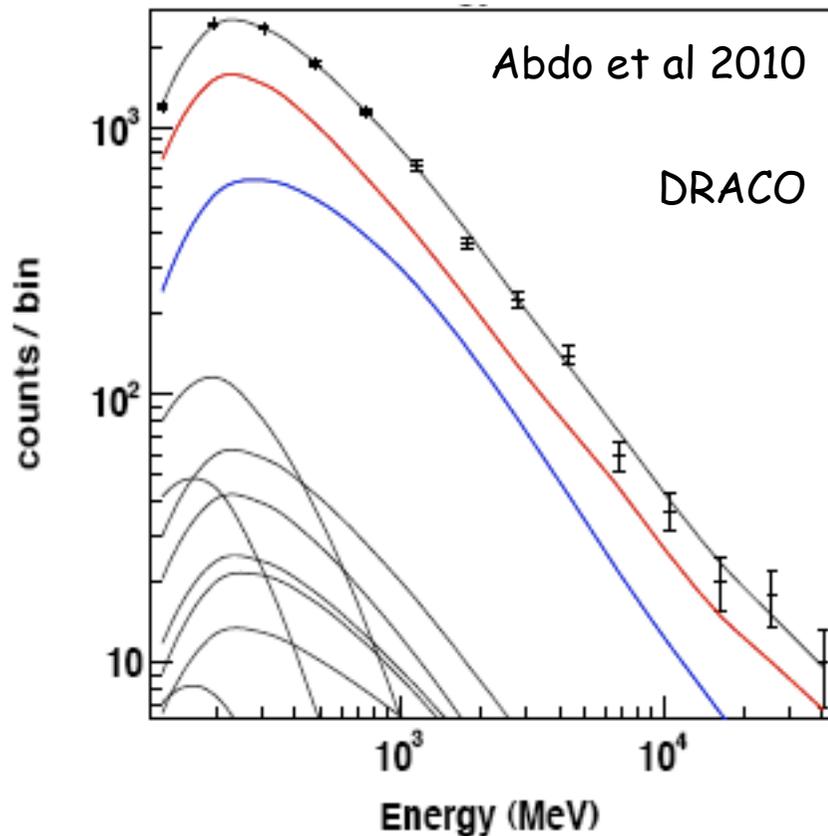
# Computing $\Phi_\gamma = \Phi_{\text{particle physics}} \times \Phi_{\text{cosmology}}$

$$\Phi_{\text{PP}} = \frac{1}{4\pi} \frac{\sigma_{\text{ann}} v}{2m_\chi^2} \int_{E_0}^{m_\chi} \sum_f \frac{dN_f^\gamma}{dE_\gamma} \text{BR}_f dE_\gamma$$



## Comparing predictions with Fermi performances

$$\text{DRACO } \Phi_{\gamma}^{\text{max}} (> 100 \text{ MeV}) = (4.5 \pm 1.5) \times 10^{-11} \text{ cm}^{-2} \text{ s}^{-1}$$

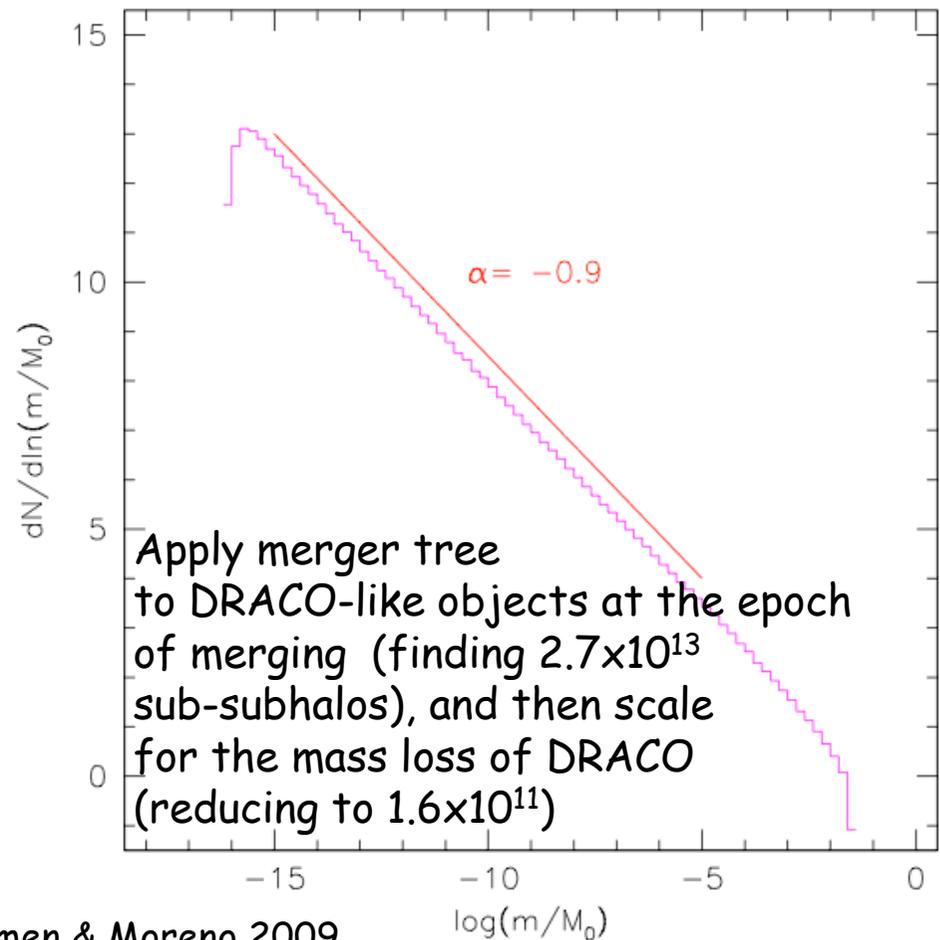
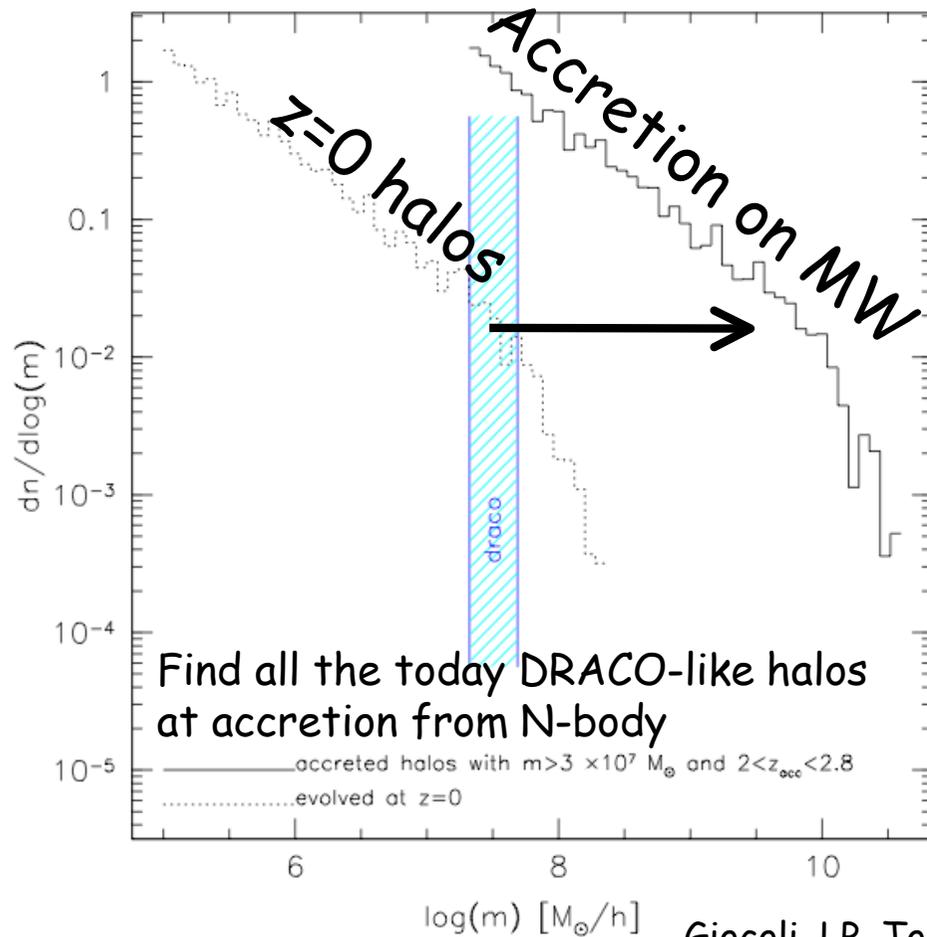
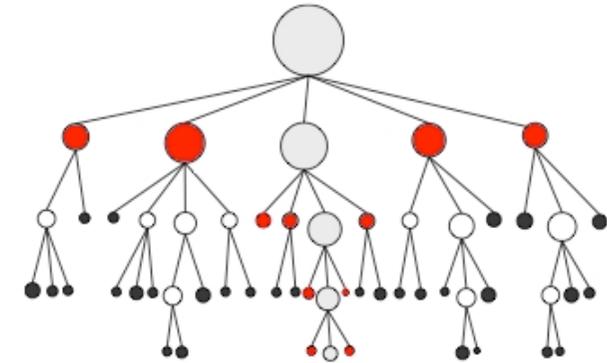


$$\Phi_{\gamma, \text{Fermi}}^{95\% \text{CL}} (> 100 \text{ MeV}, 1 \text{ yr}) \\ (0.1 - 2) \times 10^{-9} \text{ cm}^{-2} \text{ s}^{-1}$$

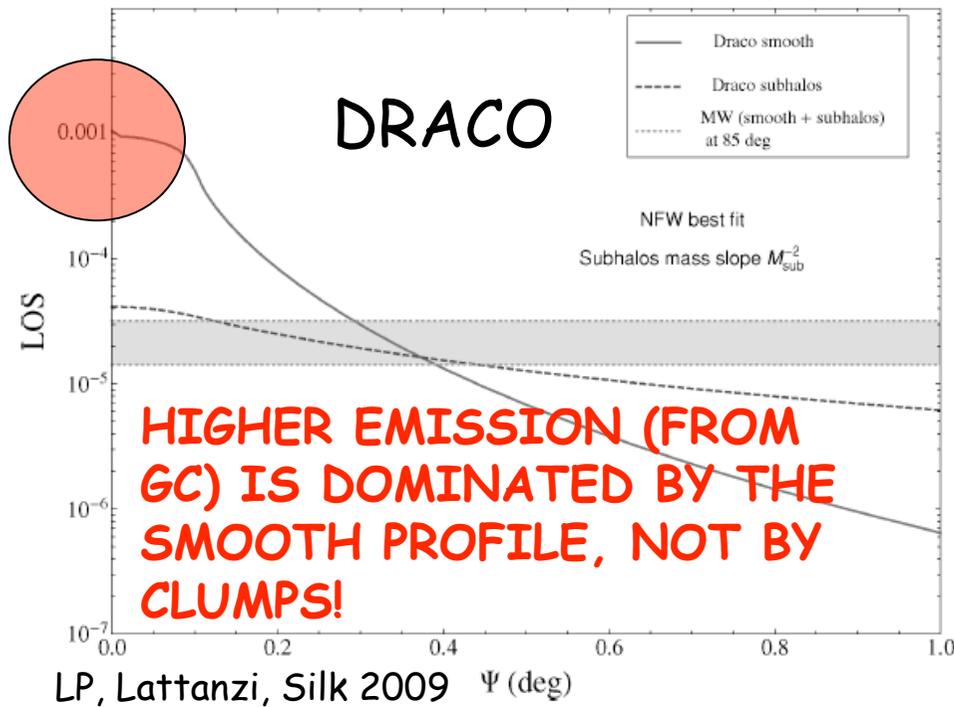
DRACO and other  
dwarfs are now only slightly  
below the detection limit  
(for our PP scenarios)

And very clean astro-objects  
poor astrophysical background  
**stable astrophysical  
predictions**

Can an astrophysical boost factor affect our computation?

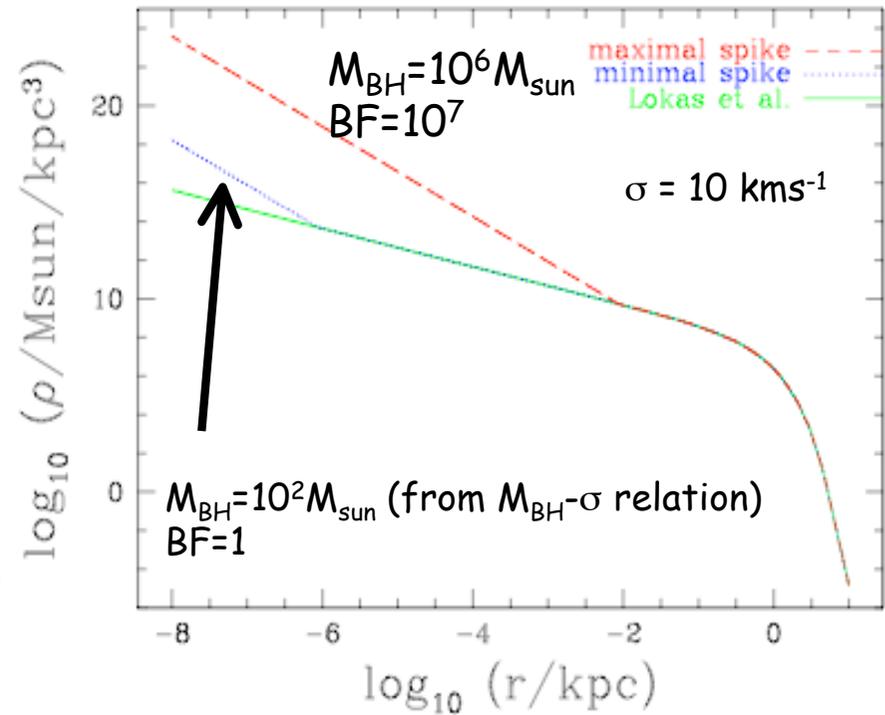


# Stability of Draco predictions: boost factors?



NFW fit to DRACO  
velocity dispersion  
(Walker et al 2008)  
 $M = 5 \times 10^9 M_{\text{sun}}$   
 $c = 22, r_s = 2 \text{ kpc}$   
 $\rho_s = 2.16 \times 10^7 M_{\text{sun}} \text{ kpc}^{-3}$

LP, Pizzella, Corsini, Dalla Bontà & Bertola 2008



A Black Hole, if any,  
is not likely to give  
any significant boost

# Conclusions

N-body simulations and theory of structure formation have allowed us to model the galactic structure and to infer predictions useful for DM detection

The inclusion of baryons in N-body simulations and the advent of new astrophysical and hopefully accelerator data could soon shade light on DM