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Physics and Signatures  
of  
Extra Dimensions

TeV Particle Astrophysics

Venice, 27-31 August 2007

## OUTLINE

- Motivations
- Framework of low scale strings  
large extra dimensions, low scale gravity
- Exp predictions for particle accelerators  
strong gravity, TeV dimensions, string effects
- D-brane embedding of the Standard Model  
unification, proton stability, Right-neutrinos
- SUSY in the bulk  $\Rightarrow$  short-range forces  
and microgravity experiments  
radion force, gauge bosons in the bulk

Hierarchy problem: why gravity is so weak compared to the other interactions?

Quantum theory: all particle masses  $\nearrow M_P \sim 10^{19}$  GeV

- TeV strings: low UV cutoff

$$\Rightarrow M_s \sim \text{TeV}$$

- Framework of type I string theory

$\Rightarrow$  D-brane world

Natural separation of  
global SUSY from gravity

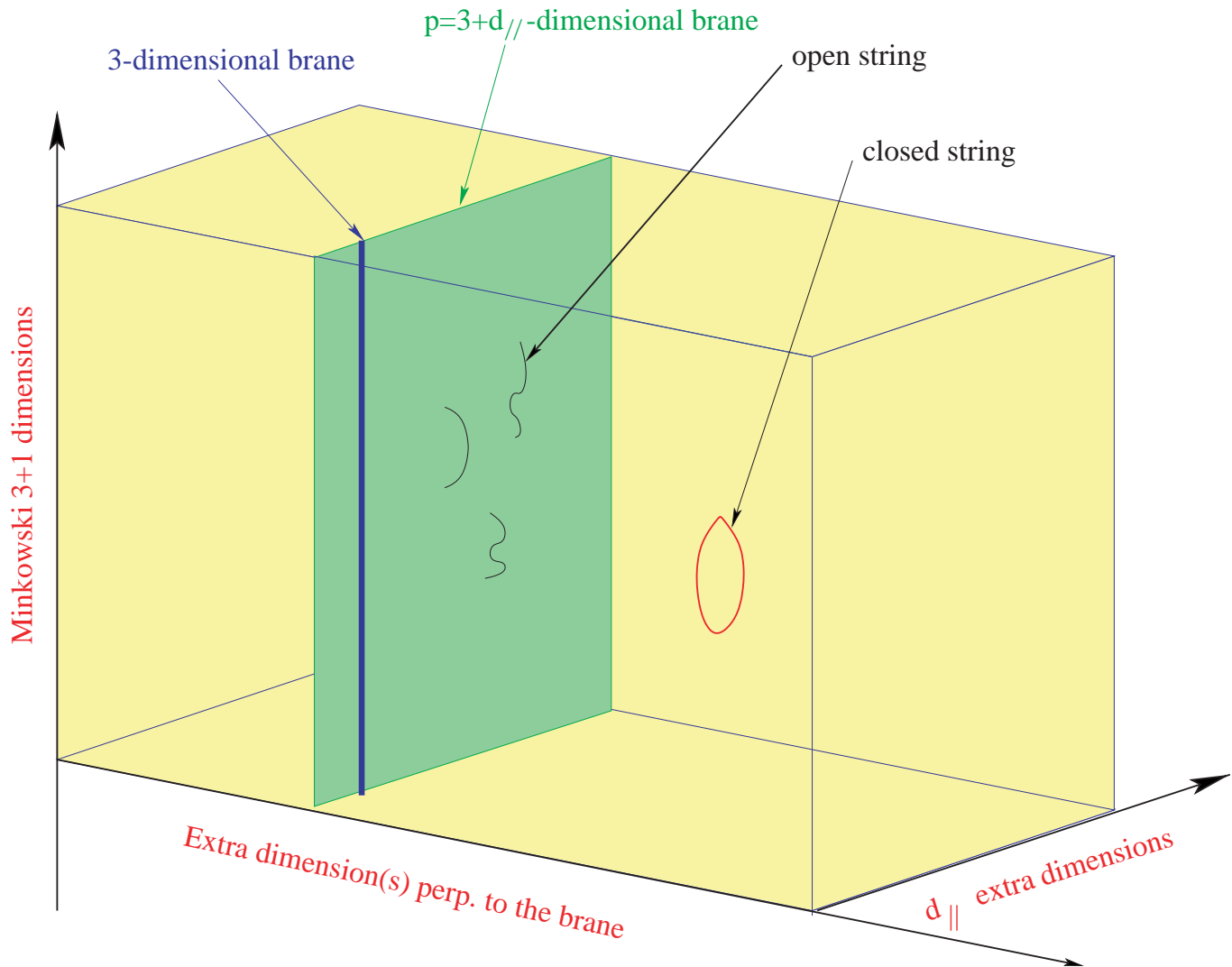


D-branes/open strings



closed strings

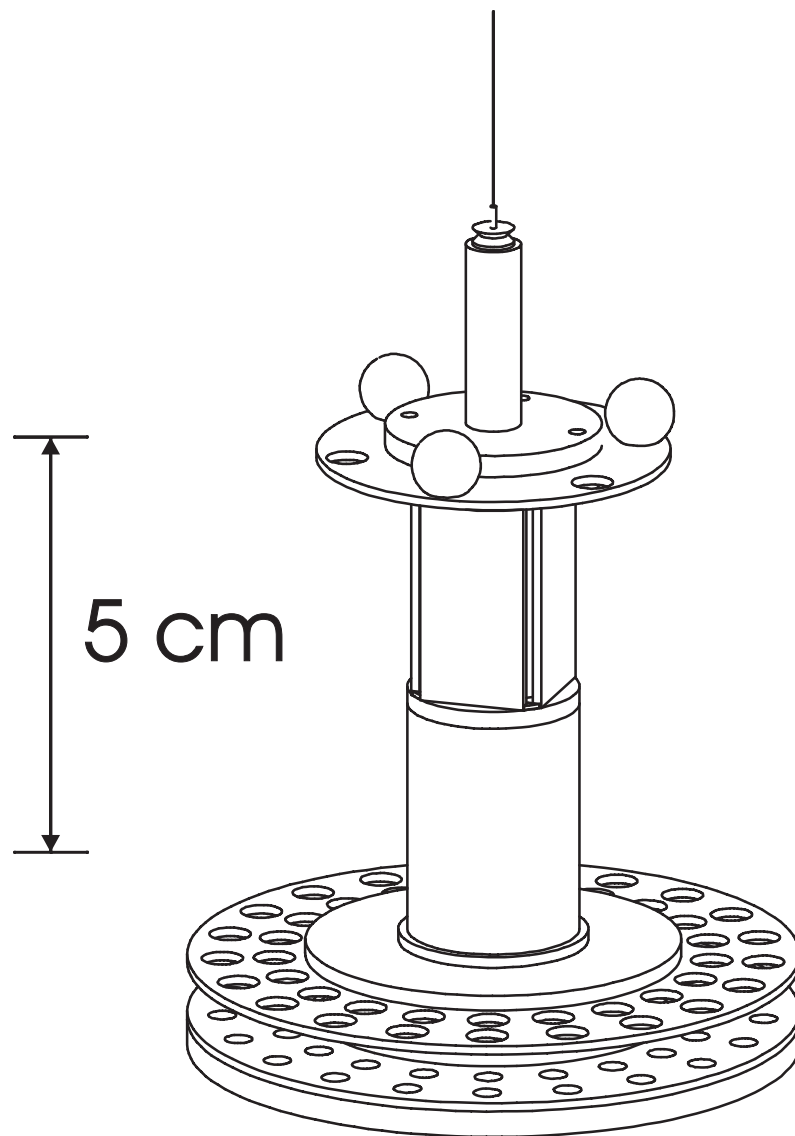
# Braneworld



two types of compact extra dimensions:

- parallel ( $d_{||}$ ): can be as large as  $10^{-16}$  cm ( $\text{TeV}^{-1}$ )
- transverse ( $\perp$ ): can be as large as 0.1 mm

Adelberger et al. '06



$R_{\perp} \lesssim 45 \mu\text{m}$  at 95% CL

- dark-energy length scale  $\approx 85 \mu\text{m}$

Dimensions of finite size:  $p - 3$  parallel

$n = 9 - p$  transverse

calculability  $\Rightarrow R_{\parallel} \simeq l_{\text{string}} ; R_{\perp}$  arbitrary

$$M_P^2 \simeq \frac{1}{\alpha^2} M_s^{2+n} R_{\perp}^n$$



Planck mass in  $4 + n$  dims:  $M_*^{2+n}$

small  $M_s/M_P \Rightarrow$  extra-large  $R_{\perp}$

$$M_s \sim 1 \text{ TeV} \Rightarrow R_{\perp} \sim .1 - 10^{-13} \text{ mm } (n = 2 - 6)$$

I.A.-Arkani Hamed-Dimopoulos-Dvali '98

- weak string coupling:  $g_s = \alpha$
- gravity strong at  $M_* \sim M_s \ll M_P$

$10^{30}$  stronger than thought previously!

deviations from Newton's law at distances  $< R_{\perp}$

## Supernova constraints

cooling due to graviton production

e.g.  $NN \rightarrow NN + \text{graviton}$

number of gravitons:  $\sim (TR_{\perp})^n$   $T \gg R_{\perp}^{-1}$   
 $\sim 10 \text{ MeV}$

$\Rightarrow$  production rate:

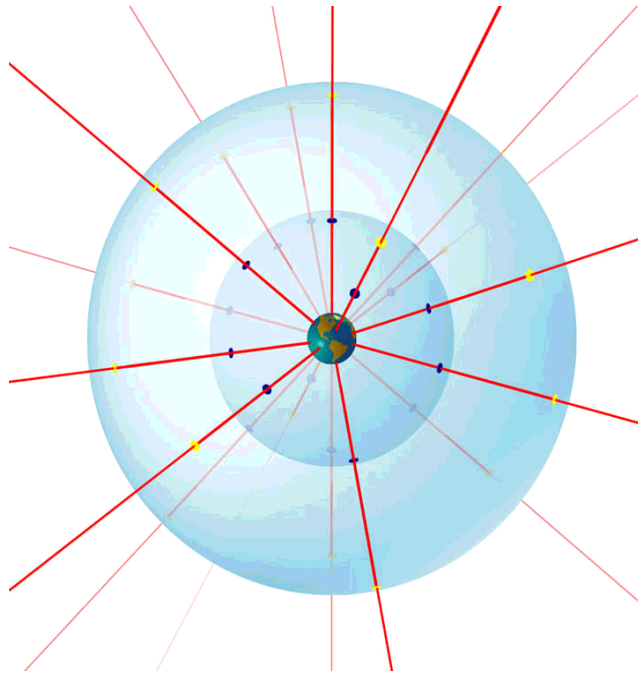
$$P_{\text{gr}} \sim \frac{1}{M_p^2} (TR_{\perp})^n \sim \frac{T^n}{M_*^{(2+n)}}$$

$$P_{\text{gr}} < P_{\nu} \Rightarrow M_* \Big|_{n=2} \gtrsim 50 \text{ TeV}$$

$$\Rightarrow M_s \gtrsim 10 \text{ TeV}$$

# Gravity modification at submillimeter distances

**Newton's law:** force decreases with area



3d: force  $\sim 1/r^2$

$(3+n)$ d: force  $\sim 1/r^{2+n}$

observable for  $n = 2$ :  $1/r^4$  with  $r \lesssim .1$  mm



Hidden submillimeter dimensions

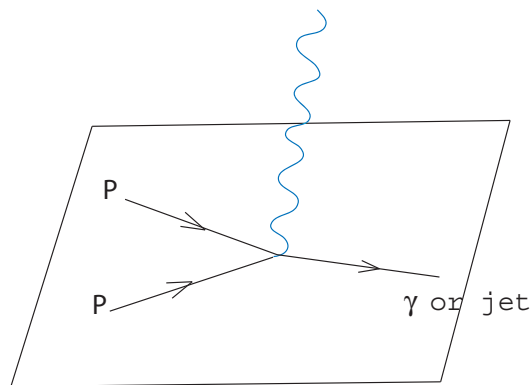
⇒ strong gravity at the TeV

Gravitational radiation in the bulk

3d: Kaluza Klein gravitons very light

⇒ high energy: huge number of particles produced

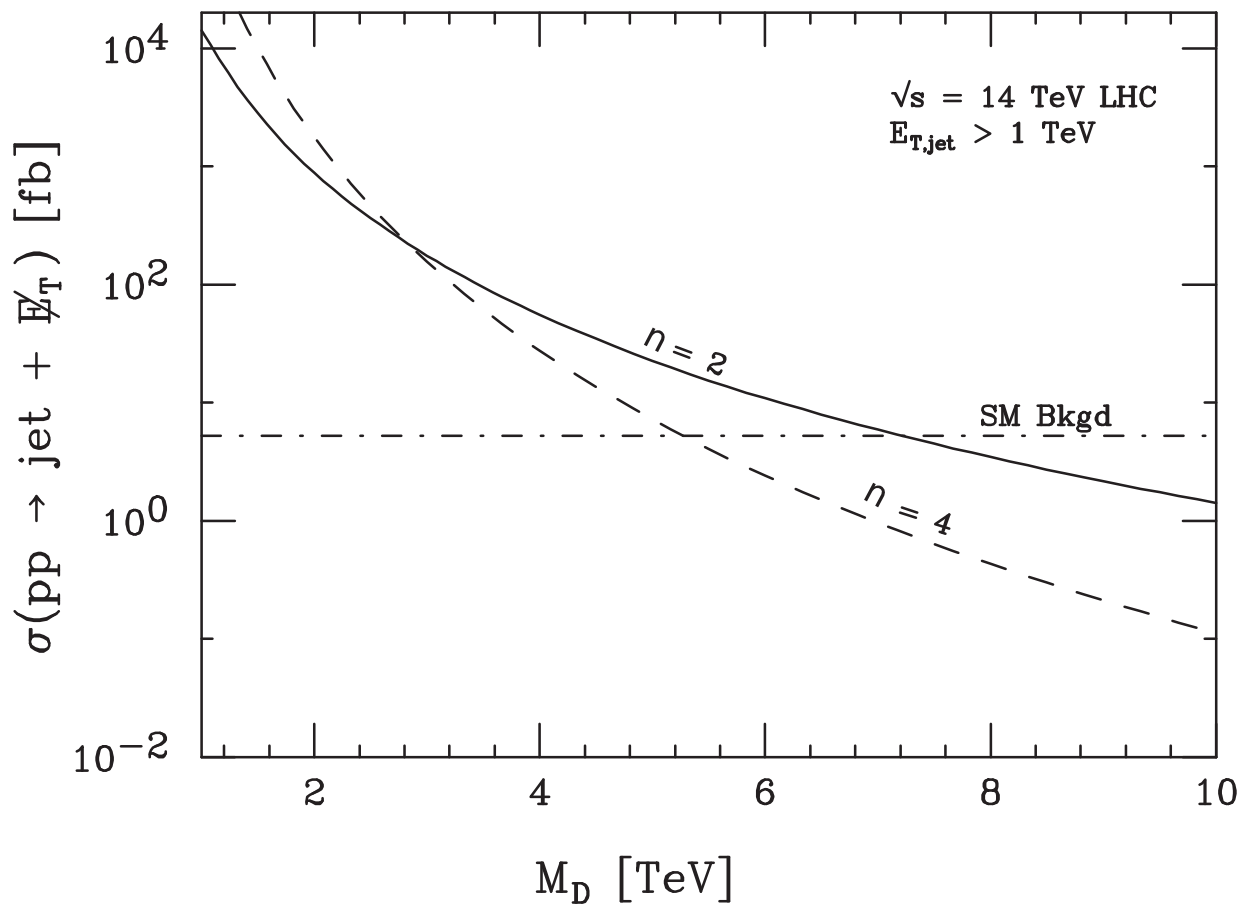
LHC:  $10^{30}$  massive gravitons of intensity  $10^{-30}$  each



Signal: missing energy

Angular distribution ⇒ spin of the graviton

Giudice-Rattazzi-Wells '98



no observation  $\Rightarrow$

$$R_{\perp} \lesssim 10^{-2} - 10^{-12} \text{ mm } (n = 2 - 6); 95\% \text{ CL}$$

- more dimensions  $\Rightarrow$  weaker limits

## Limits on $R_{\perp}$ in mm

Experiment	$R_{\perp}(n = 2)$	$R_{\perp}(n = 4)$	$R_{\perp}(n = 6)$
<b>Collider bounds</b>			
LEP 2	$4.8 \times 10^{-1}$	$1.9 \times 10^{-8}$	$6.8 \times 10^{-11}$
Tevatron	$5.5 \times 10^{-1}$	$1.4 \times 10^{-8}$	$4.1 \times 10^{-11}$
LHC	$4.5 \times 10^{-3}$	$5.6 \times 10^{-10}$	$2.7 \times 10^{-12}$
NLC	$1.2 \times 10^{-2}$	$1.2 \times 10^{-9}$	$6.5 \times 10^{-12}$
<b>Astrophysics/cosmology bounds</b>			
SN1987A	$3 \times 10^{-4}$	$1 \times 10^{-8}$	$6 \times 10^{-10}$
COMPTEL	$5 \times 10^{-5}$	-	-

## Large TeV dimensions

longitudinal dimensions:  $R^{-1} \lesssim M_s \Rightarrow$

$R^{-1}$  first scale of new physics I.A. '90

increasing the energy

- could happen for some of the internal dims
- explain coupling constant ratios  $g_2/g_3$
- susy breaking
- fermion masses displace light generations

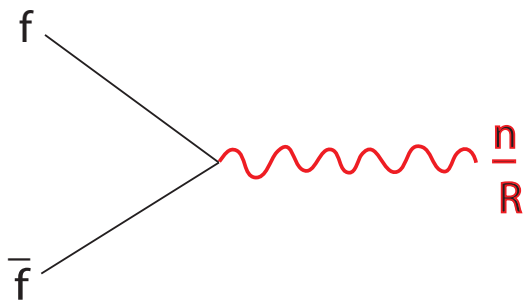
Massive tower of Kaluza Klein modes  
for Standard Model particles

$$M_n^2 = M_0^2 + \frac{n^2}{R^2} \quad ; \quad n = \pm 1, \pm 2, \dots$$

$\Rightarrow$  excited states of photon,  $W^\pm$ ,  $Z$ , gluons

## Localized fermions (on 3-brane intersections)

⇒ single production of KK modes

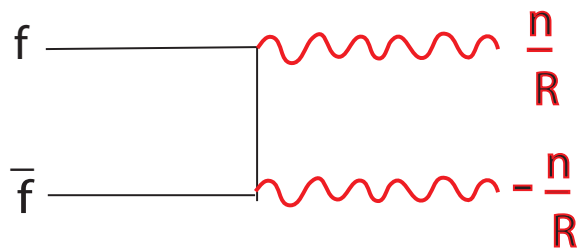


I.A.-Benakli '94

- strong bounds indirect effects:  $R^{-1} \gtrsim 3\text{TeV}$
- new resonances but at most  $n = 1$

## Otherwise KK momentum conservation

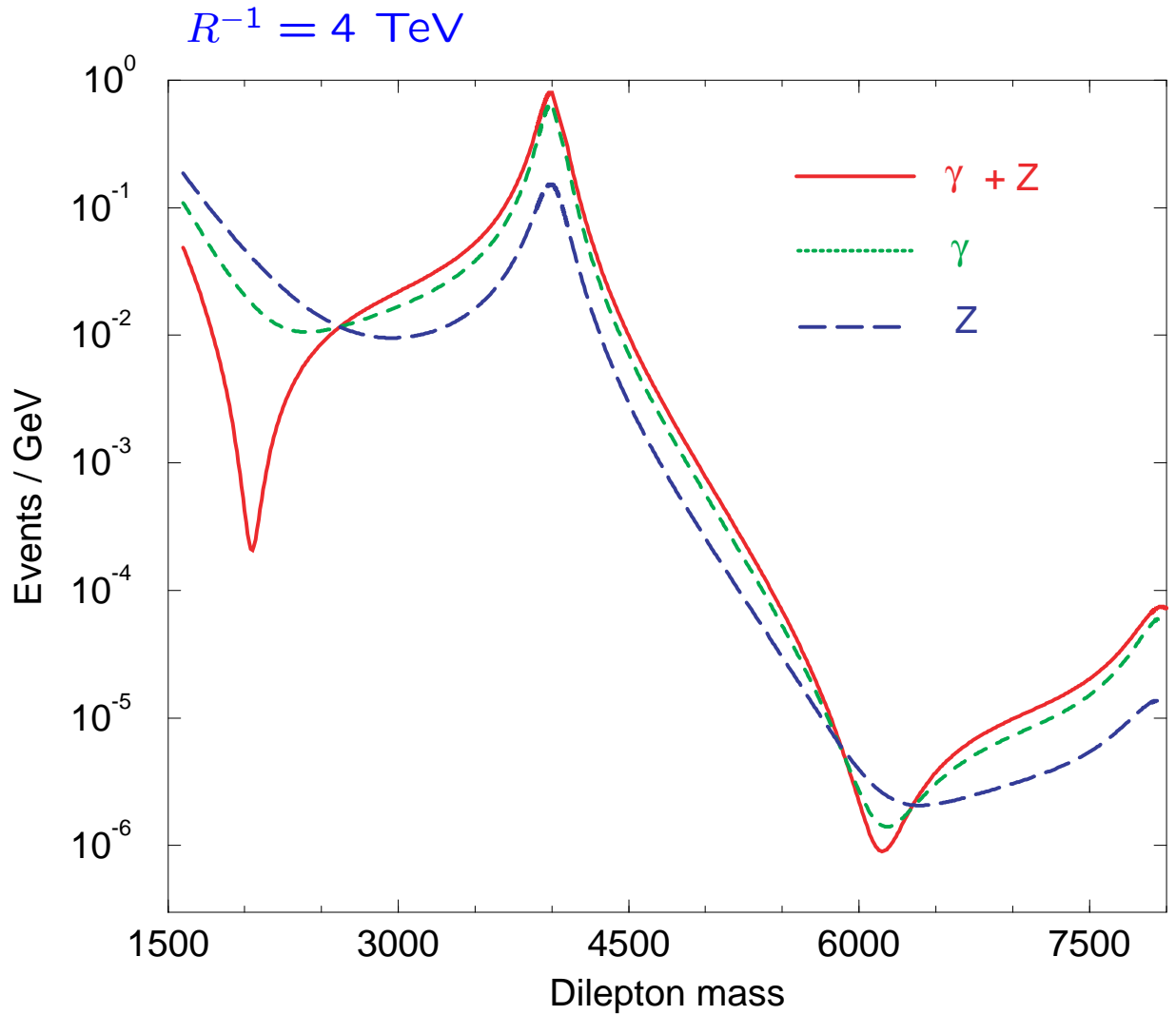
⇒ pair production of KK modes (universal dims)



- weak bounds  $R^{-1} \gtrsim 300\text{-}500\text{ GeV}$
- no resonances
- lightest KK stable ⇒ dark matter candidate

Servant-Tait '02

I.A.-Benakli-Quiros '94, '99



- no observation in dijets

$$\Rightarrow R^{-1} \gtrsim 20 \text{ TeV ; 95\% CL}$$

- more than one dimension  $\Rightarrow$  stronger limits

Massive string vibrations  $\Rightarrow$  indirect effects

virtual exchanges  $\Rightarrow$  effective interactions

e.g. four-fermion operators

Actual limits: Matter fermions on

- same set of branes  $\Rightarrow M_s \gtrsim 500$  GeV

dim-8:  $\frac{g^2}{M_s^4}(\bar{\psi}\partial\psi)^2$  Cullen-Perelstein-Peskin '00

- brane intersections  $\Rightarrow M_s \gtrsim 2 - 3$  TeV

dim-6:  $\frac{g^2}{M_s^2}(\bar{\psi}\psi)^2$  I.A.-Benakli-Laugier '00

High energies  $\Rightarrow$

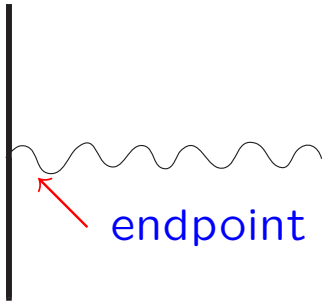
- direct production: string physics
- strong gravity: production of micro-black holes?

Giddings-Thomas, Dimopoulos-Landsberg '01

## Generic spectrum

$N$  coincident branes  $\Rightarrow U(N)$

a-stack



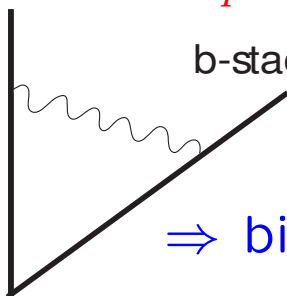
endpoint transformation:  $\mathbf{N}_a$  or  $\bar{\mathbf{N}}_a$

$U(1)_a$  charge:  $+1$  or  $-1$

$U(1)$ : “baryon” number

- open strings from the same stack  
 $\Rightarrow$  adjoint gauge multiplets of  $U(N_a)$
- open strings stretched between two stacks

a-stack in  $p$  dims



b-stack in  $p'$  dims

$\Rightarrow$  bifundamentals of  $U(N_a) \times U(N_b)$

in  $p \cap p'$  dims



## A D-brane embedding of the Standard Model

I.A.-Kiritsis-Tomaras '00

I.A.-Kiritsis-Rizos-Tomaras '02

- oriented strings  $\Rightarrow$

need at least 4 brane-stacks

- existence of bulk with large dimensions  $\Rightarrow$

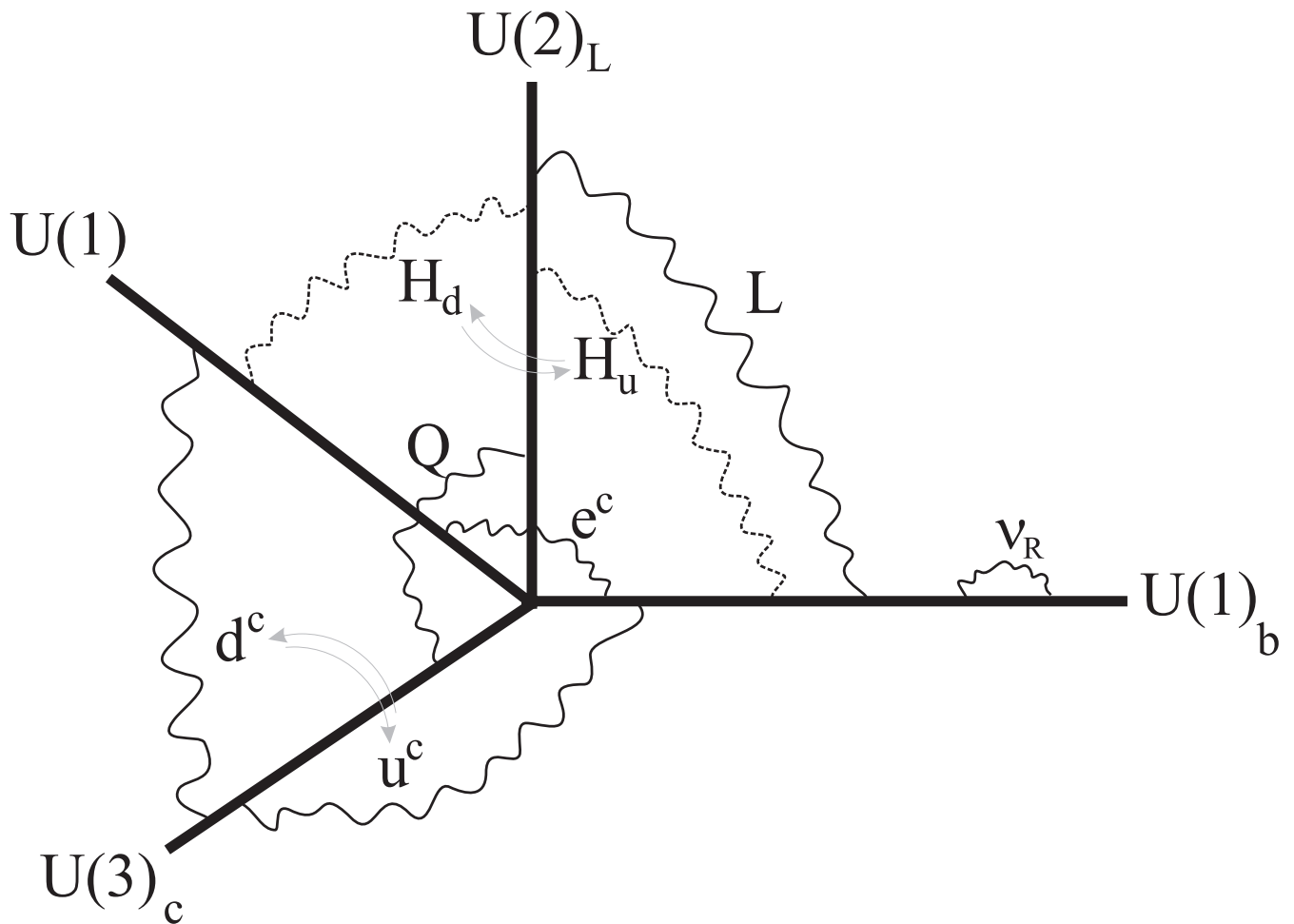
minimal choice:  $U(3) \times U(2) \times U(1) \times U(1)_{bulk}$

A diagram showing two red arrows pointing upwards from labels to terms in the group product. The left arrow points from 'color branes (g3)' to 'U(3)'. The right arrow points from 'weak branes (g2)' to 'U(2)'.  
color branes ( $g_3$ )                      weak branes ( $g_2$ )

- also for non-oriented strings

with Baryon and Lepton number symmetries

## Standard Model on D-branes



- $g_2^2/g_3^2 = R/l_s \Rightarrow$  KK modes for  $SU(2)_L$
- $U(1)^4 \Rightarrow$  hypercharge + B, L, PQ global
- $U(1)$  on top of  $U(2)$  or  $U(3) \Rightarrow$  prediction for  $\sin^2 \theta_W$
- $\nu_R$  in the bulk  $\Rightarrow$  small neutrino masses

The remaining three  $U(1)$ 's : anomalous

Green-Schwarz anomaly cancellation  $\Rightarrow$

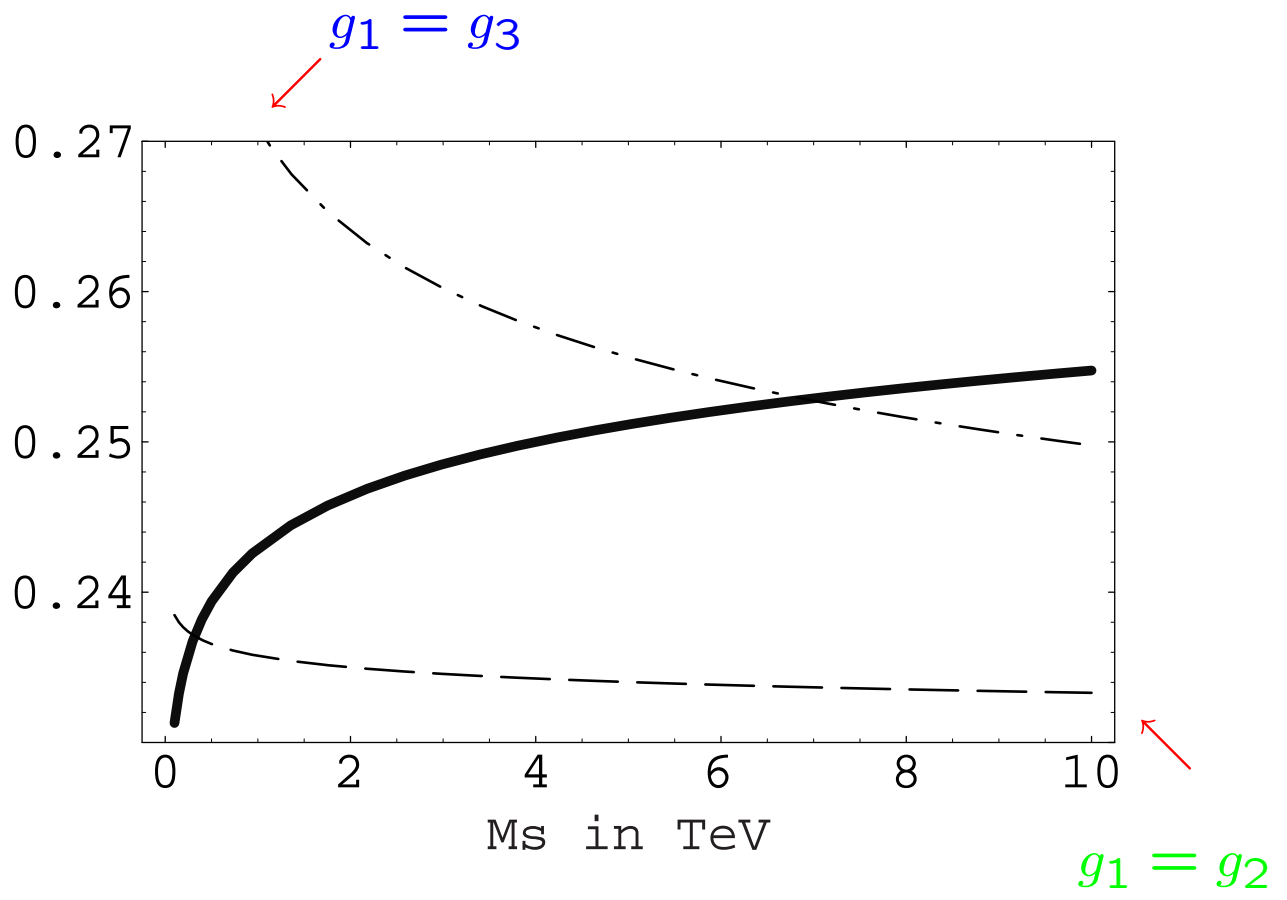
- they become massive (absorb three axions)
- the global symmetries remain in perturbation
- Baryon number  $\Rightarrow$  proton stability
- Lepton number  $\Rightarrow$  protect small neutrino masses

no Lepton number  $\Rightarrow \frac{1}{M_s} LLHH$

$\Rightarrow$  Majorana mass:  $\frac{\langle H \rangle^2}{M_s} LL$

$\sim$  GeV

$$\sin^2 \theta_W(M_s)$$



$\Rightarrow$  correct prediction for  $\sin^2 \theta_W$   
for  $M_s \sim$  a few TeV

## R-neutrinos: open strings in the bulk

Arkani Hamed-Dimopoulos-Dvali-March Russell '98

Dienes-Dudas-Gherghetta '98

$$\bullet \int d^{4+n}x \bar{\nu} \not{\partial} \nu \quad \nu = (\nu_R, \nu_R^c) \Rightarrow$$

$$R_{\perp}^n \int d^4x \sum_m \left\{ \bar{\nu}_{Rm} \not{\partial} \nu_{Rm} + \bar{\nu}_{Rm}^c \not{\partial} \nu_{Rm}^c + \frac{m}{R_{\perp}} \nu_{Rm} \nu_{Rm}^c + c.c. \right\}$$

$$\bullet S_{int} = g_s \int d^4x H(x) L(x) \nu_R(x, y=0)$$

$$\langle H \rangle = v \Rightarrow \text{mass-terms: } \frac{g_s v}{R_{\perp}^{n/2}} \sum_m \nu_L \nu_{Rm}$$

$$\frac{g_s v}{R_{\perp}^{n/2}} \ll \frac{1}{R_{\perp}} \Leftrightarrow g_s v \ll R_{\perp}^{n/2-1} \Rightarrow$$

-  $m \neq 0$ : masses for KK  $\nu_m$  unaffected

-  $m = 0$ : Dirac neutrino masses

$$m_{\nu} \simeq \frac{g_s v}{R_{\perp}^{n/2}} \simeq v \frac{M_s}{M_p}$$

$$\simeq 10^{-3} - 10^{-2} \text{ eV for } M_s \simeq 1 - 10 \text{ TeV}$$

- global SUSY: no need to be there  
at least for hierarchy
- SUGRA: probably unbroken in the bulk  $\Rightarrow$   
very weakly broken

New forces at submm scales

e.g. radion, gauge fields

Radion  $\equiv \ln V_{\perp}$

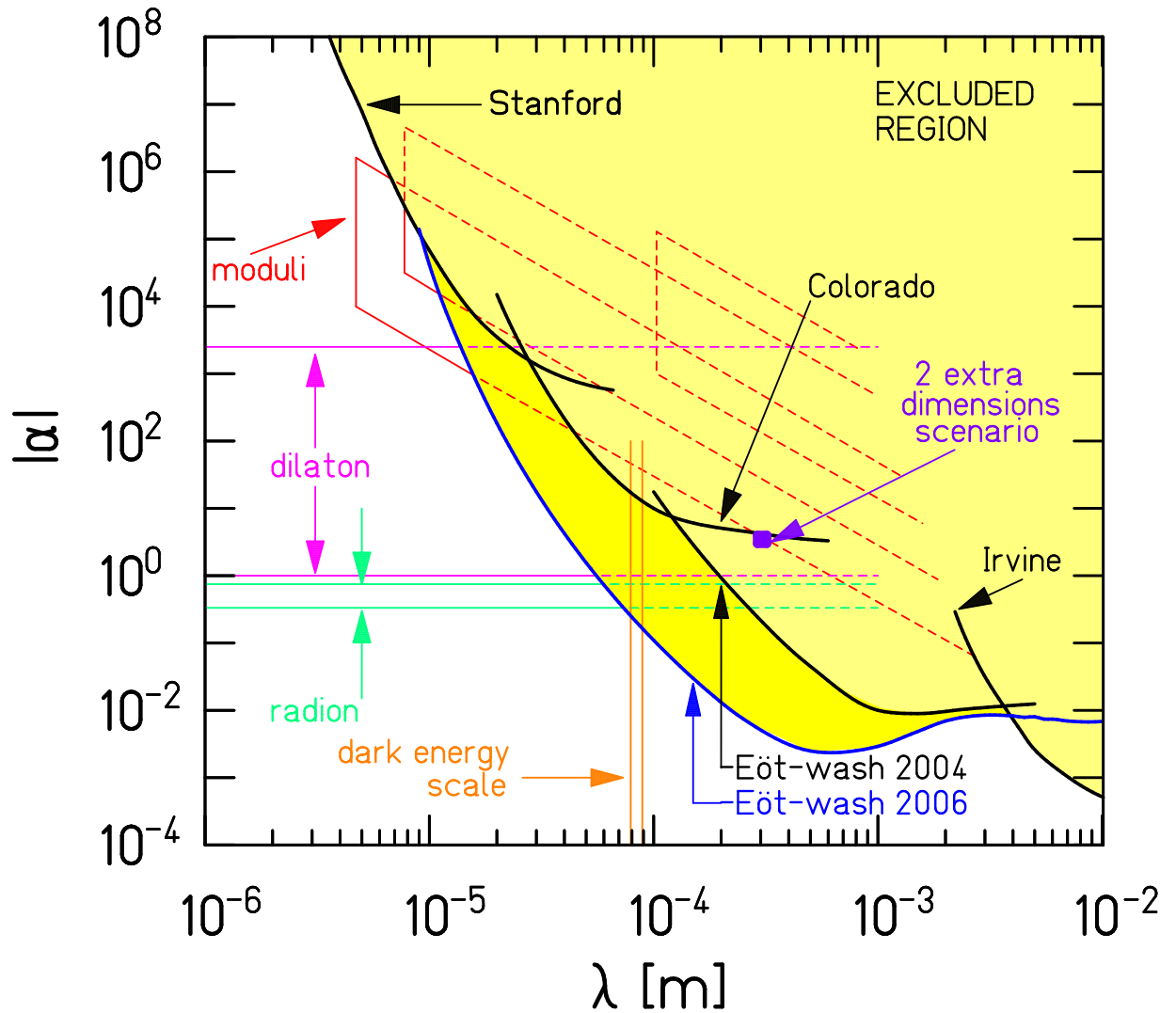
mass:  $(\text{TeV})^2/M_P \sim 10^{-4} \text{ eV} \rightarrow \text{mm range}$

coupling:  $\frac{1}{m} \frac{\partial m}{\partial \ln V_{\perp}} = \sqrt{\frac{n}{n+2}} \times \text{gravity}$

$\Rightarrow$  can be experimentally tested for all  $n \geq 2$

I.A.-Benakli-Maillard-Laugier '02

$$V(r) = -G \frac{m_1 m_2}{r} \left( 1 + \alpha e^{-r/\lambda} \right)$$



Radion  $\Rightarrow M_* \gtrsim 6 \text{ TeV}$  95% CL

Adelberger et al. '06

Light  $U(1)$  gauge bosons

$$m_A = g_A M$$

small mass  $\Rightarrow$  small coupling

$\Rightarrow A$  in the bulk with localized mass

$$g_A \sim 1/\sqrt{V_\perp}$$

$$\Rightarrow m_A \gtrsim M_s^2/M_P \simeq 10^{-4} \text{ eV}$$

$A$  propagates in part of the bulk

$\Rightarrow$  new submm forces

$$g_A \sim 1/\sqrt{V_\perp} \gtrsim M_s/M_P \sim 10^{-16}$$

$\Rightarrow \gtrsim 10^6 - 10^8 \times$  gravity

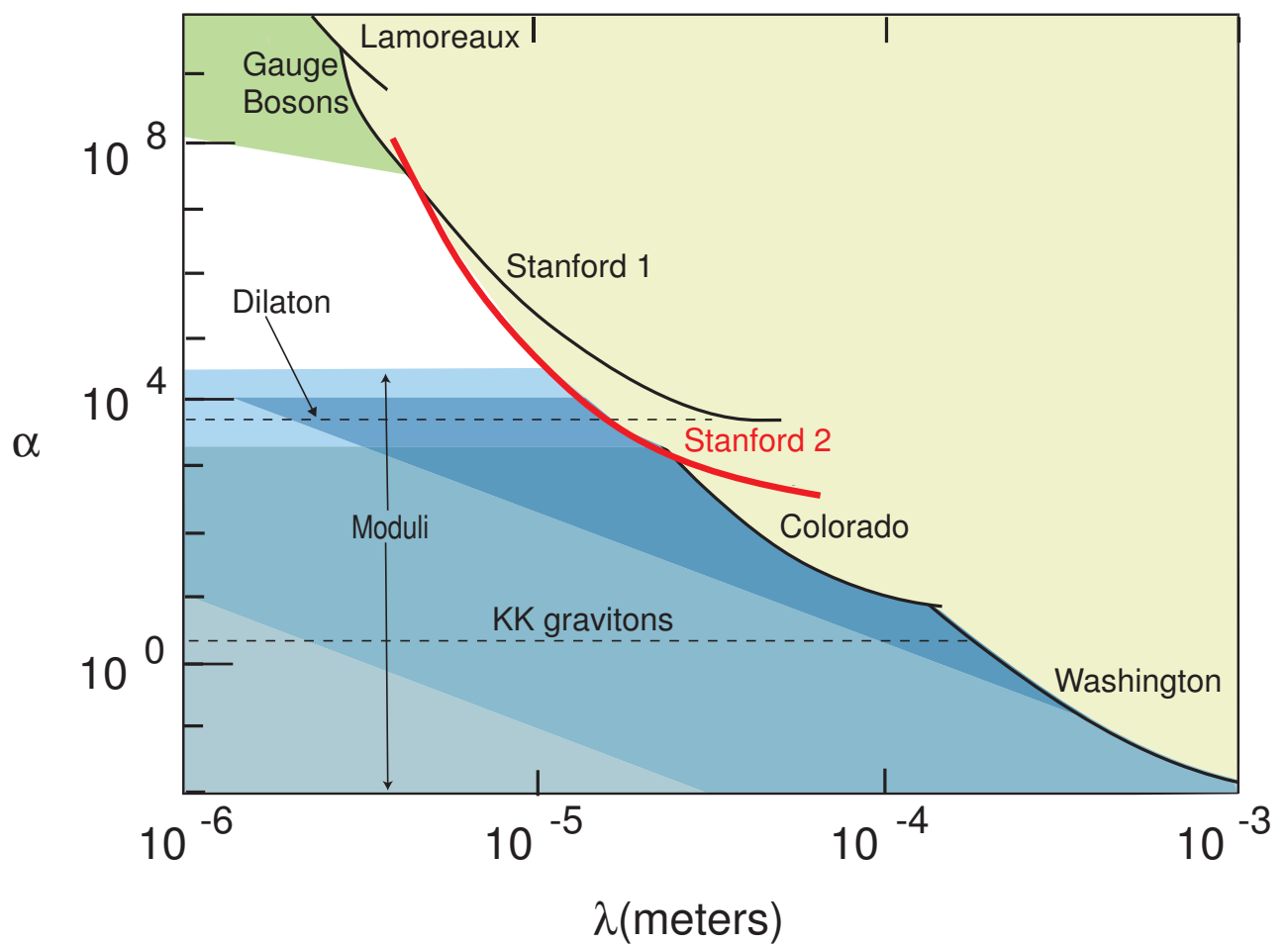
$m_{\text{proton}}/M_*$

supernova  $\Rightarrow$  dim of the bulk  $\geq 4$



an order of magnitude improvement  
on bounds in the range 6-20  $\mu\text{m}$

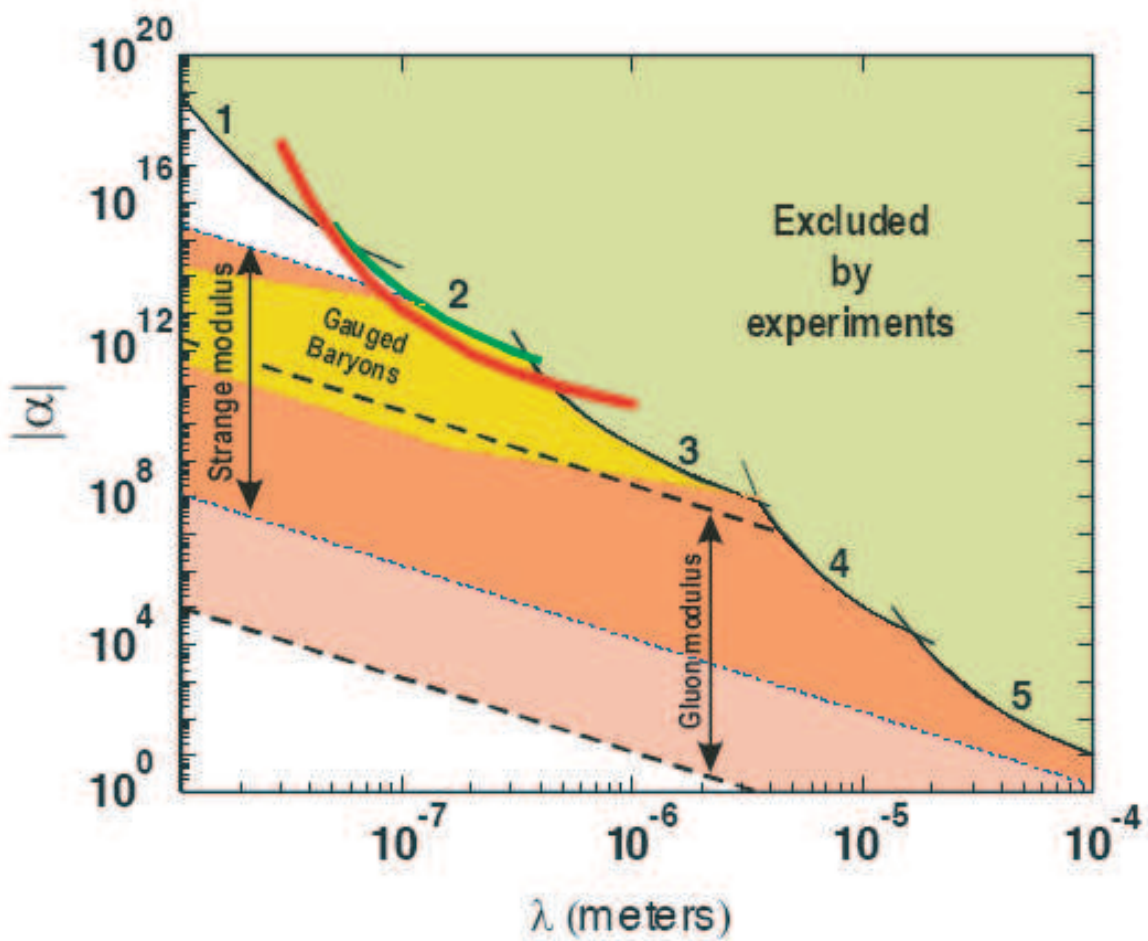
Smullin-Geraci-Weld-Chiaverini-Holmes-Kapitulnik '05



Casimir effect: an order of magnitude improvement  
on bounds in the range 10-200 nm

Decca-López-Chan-Fischbach-Krause-Jamell '05

Decca et al. '07



5: Colorado

4: Stanford

3: Lamoureaux

1: Mohideen et al.

## Conclusions

TeV strings and large extra dimensions:

Physical reality or imagination?

Well motivated theoretical framework

with many testable experimental predictions

new resonances, missing energy

Stimulus for micro-gravity experiments

look for new forces at short distances

higher dim graviton, scalars, gauge fields

LHC: will explore the physics beyond  
the Standard Model